

SINGLE-PHASE GRID-CONNECTED PHOTOVOLTAIC SYSTEM WITH ACTIVE POWER LINE CONDITIONING

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Abstract – This paper deals with an alternative current reference generator algorithm proposition, which is employed to inject active power into the grid and, simultaneously, performs reactive power compensation and load harmonic current suppression in single-phase grid-connected photovoltaic (PV) systems. The PV system reference current is computed based on synchronous reference frame method, which operates in conjunction with the dc-bus controller. In addition, by adopting a proper strategy, it is proposed criteria for establishing the priority on the power compensation by the PV system, in order that the power rating of the grid-connected PWM converter is not exceeded. The Perturb-and-Observe maximum power point tracking technique is employed to generate the dc-bus voltage reference for extracting the maximum power from the photovoltaic array and, therefore, maximizing its efficiency. Both simulation and experimental results are presented to verify the static and dynamic behaviors of the grid-tied photovoltaic system, as well as evaluate its performance.

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Keywords – Active Power Filter, Harmonic Suppression, Photovoltaic System, Power Quality, Reactive Power Compensation.

I. INTRODUCTION

In the last years, studies related to alternative and renewable energy sources have grown significantly [1], due to the increasing demand for electrical energy, and mainly because of the reduction of ecological and economic impacts. Hydropower, biomass, wind, sea and solar, arise among the several alternative and renewable energy sources. Considering this scenario, the solar energy can be considered the most useful of the available renewable energy sources.

After its conversion in electrical energy, by means of photovoltaic (PV) arrays, the solar energy can be injected into the utility grid by using proper energy conversion stages. Normally, for this purpose, it is performed by means of dc/dc and dc/ac converters. The first is used to step-up the PV array voltage, while the second is used to connect the PV system to the utility grid [2]-[5]. In many PV systems, the dc/dc conversion stage is suppressed, and the energy provided from the PV arrays is directly injected into the grid by using of dc/ac converter only [6]-[12].

On the other hand, the implementation of PV systems with filtering capabilities has been justified because the current

and/or voltage harmonic distortions have risen significantly in the power supply systems [10]-[15]. This problem has happened due to the increasing use of nonlinear loads, such as switching power supplies, inverters, rectifiers, among others, which are normally used in industrial, commercial and residential applications.

Since nonlinear loads have contributed for the generation of significant harmonic contents in the grid, they appear as the main responsible by changing the sinusoidal utility voltage characteristics, contributing for the power quality (PQ) degradation. Thus, when the harmonic currents interact with the utility impedance, result in voltage harmonic distortions that can affect the PQ of the consumers connected in the same electrical system point of common coupling. Additional effects can be seen through the excessive heating of transformers and electrical equipment, increasing noise in the audible frequency, and electromagnetic torque oscillations in electric motors [16].

Shunt active power filter (APF) arises as an alternative means to minimize some PQ problems. They have been used to eliminate or mitigate the effects on the power system caused by the circulation of harmonic currents created by nonlinear loads [17]-[19].

Considering single- and three-phase systems several grid-tied photovoltaic systems with active filtering capability have been proposed in literature [10]-[13], using different strategies to perform the following purposes: i. injecting active power to the grid; ii. compensating of the load reactive power; and iii. suppressing of the load harmonic currents.

This paper proposes an alternative power-line conditioning algorithm implemented through the current reference generator (CRG), which is used to control the single-phase grid-tied photovoltaic and active power filter (PV-APF) system shown in Figure 1. The PV-APF system is connected to the utility grid by means of a current controlled full-bridge (1F-B) single-phase pulse width modulation (PWM) converter connected to the grid using a coupling inductor (L-filter) [11]-[13]. A simple algorithm is adopted to obtain the current reference, which is synthesized by the 1F-B converter. Thereby, the PV-APF current reference is obtained by using the method based on synchronous reference frame (SRF) operating in conjunction with the dc-bus controller. In this case, the compensation current, composed of reactive and harmonic currents, is generated by the SRF-based algorithm, while the active current, obtained from the PV array, is generated by the dc-bus controller operating together with a phase-locked loop (PLL) system.

The PLL system is employed to obtain the synchronization between the PV-APF system and the utility grid [20], [21]. In addition, it is also used for generating the

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coordinates of the synchronous unit vector $\sin(\theta_{pll})$ and $\cos(\theta_{pll})$, which are used in the PV-APF current reference generator, such that θ_{pll} must be equal to the estimated utility phase-angle θ .

On the other hand, the power processed to perform the load reactive power compensation and the current harmonic suppression must be monitored such that the nominal power rating of the PWM converter is not exceeded. For this reason, it is proposed a calculation algorithm, which is used to limit the amount of power processed by the converter, in order that its rated current remains within the designed limits.

Some PV array models have been proposed in literature [23]-[26]. In this paper, the simulations involving the PV array is implemented by means of the equivalent electrical model proposed in [25], [26]. The PV-APF system is composed of ten modules connected in series resulting a maximum output voltage around 308 V in the dc-bus of the PV array, which operates at Maximum Power Point (MPP) under the Standard Test Conditions (STC). Thus, it is possible the direct connection between the PV array and the 1F-B converter dc-bus (Figure 1). Hence, the step-up stage is not needed [27], [28], increasing the overall system efficiency [29].

Mathematical analyses are presented, as well as simulation and experimental results are shown to evaluate both static and dynamic performance of the PV-APF system, validating the theoretical development.

II. CHARACTERISTICS OF THE GRID-TIED PV-APF SYSTEM

The complete PV-APF system is shown in Figure 1, where the PV arrangement is composed of ten panels connected in series providing maximum PV array output power around 2.4 kW.

In the next subsections the following subjects are described: i. the equivalent PV model; ii. the implemented MPPT technique operating in conjunction with the dc-bus voltage controller; iii. the algorithm used for the current reference generation; iv. the PV-APF current controller; and v. the PLL system.

A. PV Model

In this work, it is adopted in the simulations, the solar cell equivalent electrical circuit presented in [23], [26], which is represented by a current source shown in Figure 2. Thus, the PV cell output current i_{pv} is given by:

$$i_{pv} = I_{ph} - I_r \left[e^{\frac{V+i_{pv}R_s}{\eta kT}} - 1 \right] - \frac{V+i_{pv}R_s}{R_p} \quad (1)$$

where V is the output voltage at PV cell terminals; I_{ph} and I_r are the photocurrent and the reverse saturation currents, respectively; R_s and R_p are the series and shunt resistances, respectively; q is the electron charge; η is the ideality factor of the junction p-n; k is the Boltzmann constant; T represents the ambient temperature, in Kelvin; and G represents the power density of the solar radiation.

The photocurrent current I_{ph} and the reverse saturation current I_r are given respectively by:

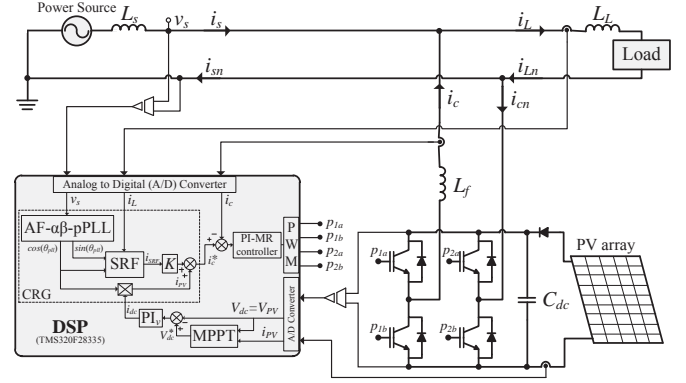


Fig. 1. Complete scheme of the single-phase grid-tied PV system.

$$I_{ph} = [I_{SC} + \alpha(T - T_r)] \frac{G}{1000} \quad (2)$$

$$I_r = I_{rr} \left(\frac{T}{T_r} \right)^3 e^{\left[\frac{qE_g}{\eta k} \left(\frac{1}{T_r} - \frac{1}{T} \right) \right]} \quad (3)$$

where T_r is the nominal temperature, in Kelvin (298 K); I_{SC} is the short circuit current at STC ($T_r = 25^\circ\text{C}$, and $G = 1000 \text{ W/m}^2$); α is the temperature coefficient; I_{rr} is the diode reverse saturation current; and E_g is the band gap energy (1.1 eV).

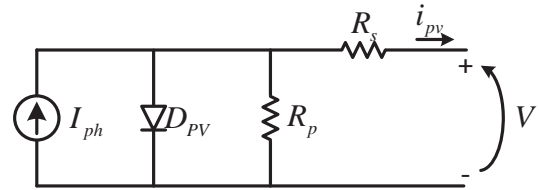


Fig. 2. Equivalent circuit of the photovoltaic cell.

The diode reverse saturation current and the PV array voltage V_{PV} are given respectively by:

$$I_{rr} = \frac{I_{SC} - \frac{V_{oc}}{R_p}}{e^{\frac{qV_{oc}}{\eta kT_r}} - 1} \quad (4)$$

$$V_{PV} = VN_s M_s \quad (5)$$

where V_{oc} is the open circuit voltage of the photovoltaic cells; N_s is the number of photovoltaic cell; and M_s is the number of the PV arrays connected in series.

In addition, the PV array open circuit voltage V_{oc_PV} is given by (6).

$$V_{oc_PV} = V_{oc} N_s M_s \quad (6)$$

The PV cell current (i_{pv}) given by (1) cannot be algebraically solved due to the nonlinear relationship between i_{pv} and V . In this case, i_{pv} is achieved by using the Newton-Raphson numeric method [30], [31].

Thus, for obtaining i_{pv} , which represents the behavior of the PV arrangement, it is used the calculation routine implemented in the PV model shown in Figure 3. The input parameters of the PV model are: output voltage (V_{PV}), power solar radiation (G), and ambient temperature (T). These parameters are obtained in Standard Test Conditions (STC) [26].

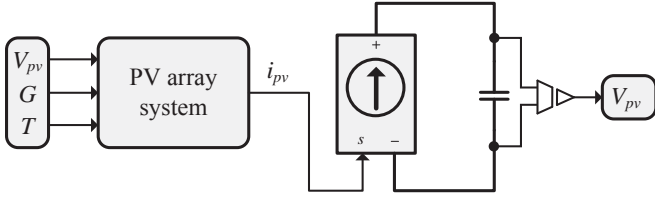


Fig. 3. Block diagram of the PV model.

B. MPPT and dc-Bus Voltage Regulation

In order to extract the maximum power from the PV array and, therefore, maximizing its efficiency, perturb-and-observe (P&O) maximum power point tracking (MPPT) technique [22] is employed as shown in Figure 4. This MPPT algorithm operates, continuously, incrementing or decrementing both the output voltage and current of the PV array. It is performed a comparison between the PV power (P_{pv}) and PV voltage (V_{pv}), obtained in the current cycle, with the respective P_{pv} and V_{pv} quantities obtained in a previous cycle. If the PV array power increases, and its voltage also increase, the control increases the voltage reference (V_{dc}^*). On the other hand, if the voltage decreases the voltage reference must decrease. An inverse logic is adopted when the PV array power decreases.

For extracting the maximum power of the PV array, the MPPT control operates incrementing or decrementing the voltage reference with a constant rate. As can be noted, the MPPT is employed to generate the PV array voltage reference (V_{dc}^*), which is used as a reference voltage in the voltage loop control shown in Figure 7.

Moreover, a proper algorithm must be used to regulate the dc-bus voltage of the PV-APF system. The dc-bus voltage is regulated according to the power available in the PV array, i.e., when the environmental conditions, such as solar radiation and temperature are favorable, the dc-bus voltage reference V_{dc}^* is set by means of the MPPT, such that V_{dc}^* is greater than 210V. In this case, the power produced by the PV array is injected into the grid.

On the other hand, for unfavorable environmental condition, in which the voltage at maximum output power conditions (V_{MPP}) in the PV array is not enough to guarantee the dc-bus voltage, the algorithm sets the dc-bus voltage reference to a constant value ($V_{dc}^* = 210$ V), in order to guarantee the system operation. The PV array reference voltage of 210 V was chosen in order to guarantee a proper operation of the converter, considering the following aspects: i. peak amplitude of the utility voltage (180 V for nominal utility rms voltage); ii. losses in both switching devices and passive components (L-filter and dc-bus capacitor); and iii. dc-bus voltage dynamic when load transients occur.

During normal operating conditions of the PV-APF system, the V_{MPP} is around 308 V ($G = 1000$ W/m², $T = 25^\circ$ C). On the other hand, taking into account a critical operation condition, such as $G = 100$ W/m² and $T = 75^\circ$ C, the V_{MPP} will be equal to 214 V.

In addition, when partial shading occurs and involves up to three PV modules, the bypass diodes will reduce the operation voltage around to 216 V. Therefore, the choice of $V_{dc}^* = 210$ V represents an acceptable voltage level, allowing an adequate operation of the PV-APF system. Thus, in this operation point, the MPPT algorithm remains operating with

constant voltage and does not extract the maximum power available in the PV array. On the other hand, the PV-APF provides active energy to the grid and can also perform load harmonic current suppression and reactive power compensation.

Thereafter, when the PV array does not have enough power to guarantee the power supply for the dc-bus voltage, the algorithm maintains the dc-bus voltage control as constant voltage, in order to guarantee the active power filtering operation only. In this case, the dc-bus voltage is controlled by the energy provided from the grid, and the PV-APF system operates as a conventional shunt APF. Thus, the active energy consumed by the load is drained from the grid.

However, as can be noted, the active energy consumed by the load can be provided from both PV-APF system and utility grid, while the PV-APF system performs, continuously, the active filtering.

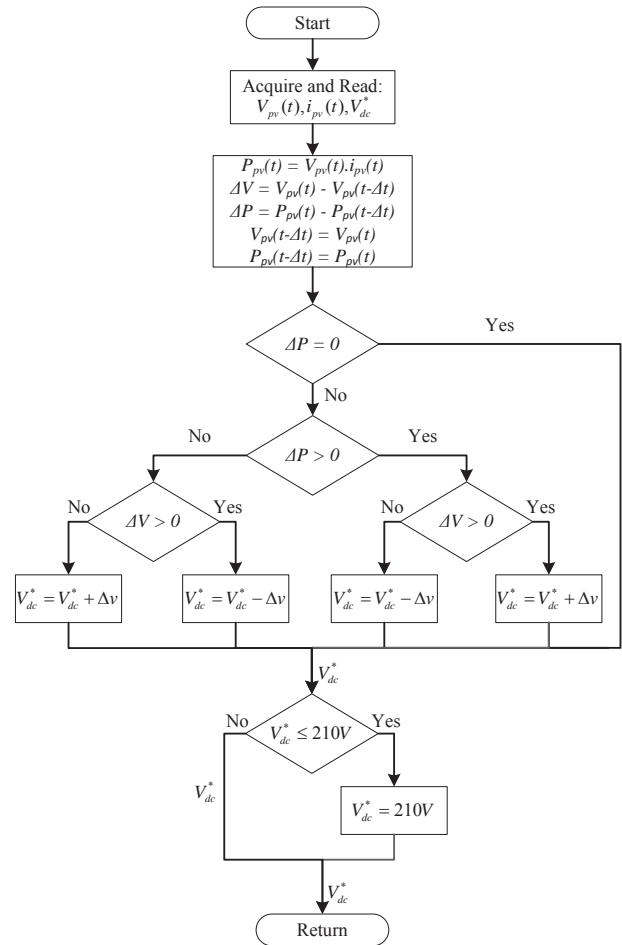


Fig. 4. Block diagram of P&O MPPT algorithm.

The voltage step size (Δv) used in the P&O algorithm must be chosen to guarantee a good performance of the system. If Δv is small, the state-steady error is reduced, however, when fast environment conditions changes occur, the algorithm can become less efficient. On the other hand, when Δv reaches large values, the losses in steady-state increases due to the oscillations around the MPP [22], [32].

Thereby, by means of a computational searching, it was possible to obtain an adequate voltage step size, such that $\Delta v = 1$ V.

The P&O algorithm runs at constant sampling time interval (T_{SMPPPT}). Similar to Δv , small values of T_{SMPPPT} lead to fast transient when solar radiation changes occur, while for large T_{SMPPPT} values the algorithm becomes slow, causing losses in the power extraction of the PV array [22], [32].

C. Generation of the PV-APF Current Reference

Several methods and theories have been proposed in order to generate the compensation current reference for shunt APF. In this paper, for this purpose, it was used an algorithm based on synchronous reference frame method. In the SRF-based algorithms, the fundamental terms of voltage and/or current of the abc -phase stationary reference frame are transformed into continuous quantities into the dq synchronous frame, in which they rotate at synchronous speed in relation to the voltage and current space vectors.

In the dq -axes, the harmonic contents of voltage and/or current can be represented by alternating quantities, which are superimposed to the continuous terms. Therefore, the fundamental components can be easily obtained by means of low-pass filters (LPFs). Phase-locked loop algorithms can be used to estimate the utility grid phase-angle, allowing the generation of the coordinates $\sin(\theta)$ and $\cos(\theta)$, that define the synchronous unit vector used in the SRF-based algorithms, where θ is the estimated phase-angle of the utility grid ($\theta = \theta_{pu}$).

The block diagram of the PV-APF current reference generator (CRG) is shown in Figure 5. In this diagram is included the SRF-based algorithm that is employed to extract the harmonic components and the reactive fundamental component of the load current, represented by id_h and $iq = iq_{dc} + iq_h$ in the synchronous rotating frame. Thus, id_h and iq_h represent the harmonic currents, and iq_{dc} represents the reactive fundamental component of the load.

Since the SRF-based algorithm was conceived to be used in balanced three-phase systems, it is necessary to create a fictitious three-phase system to allow its application in single-phase systems [19]. Therefore, the load current is measured and it is considered the actual fictitious current i_α ($i_L = i_\alpha$). Subsequently, i_α is phase-delayed in $\pi/2$ radians, producing the fictitious β coordinate (i_β). Thereby, the new fictitious two-phase stationary reference frame ($\alpha\beta$ -axes) is represented by:

$$\begin{bmatrix} i_\alpha \\ i_\beta \end{bmatrix} = \begin{bmatrix} i_L(\theta) \\ i_L(\theta - \pi/2) \end{bmatrix}. \quad (7)$$

After that, the currents i_α and i_β are transformed from the two-phase stationary reference frame into a two-phase synchronous rotating reference frame (dq -axes).

Both direct (id) and quadrature (iq) currents are obtained by means of (8), where $\sin(\theta_{pu})$ and $\cos(\theta_{pu})$ are the coordinates of the synchronous unit vector obtained from the PLL system. The dc component id_{dc} (Figure 5) represents the fundamental active current of the load, which is extracted by using a 2nd order LPF Butterworth filter.

$$\begin{bmatrix} id \\ iq \end{bmatrix} = \begin{bmatrix} \cos(\theta_{pu}) & \sin(\theta_{pu}) \\ \sin(\theta_{pu}) & -\cos(\theta_{pu}) \end{bmatrix} \begin{bmatrix} i_\alpha \\ i_\beta \end{bmatrix} \quad (8)$$

The current generated by the SRF-based algorithm i_{SRF} (Figure 5) is added to the sinusoidal PV current i_{PV} represented by:

$$i_{PV} = i_{dc} \cos(\theta_{pu}) \quad (9)$$

where i_{dc} is obtained from the dc-bus voltage controller and represents the active power flow through the PV-APF system.

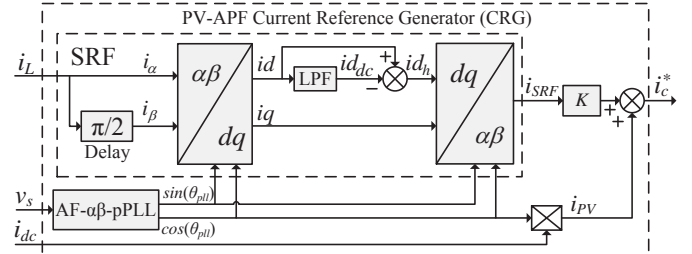


Fig. 5. Block diagram of the PV-APF current reference generator.

The quantity i_{dc} determines if the PV-APF system absorbs active power from the grid or furnishes active power into the grid. Besides, the active power generated by the PV-array, i_{dc} also represents the losses related to both the inductance filter L_f and the switching devices. In other words, i_{dc} controls the total active power demanded by the PV-APF system to regulate the dc-bus voltage.

The delay introduced into i_α to obtain the fictitious current i_β must not interfere on the dynamic response of the current obtained from the CRG. This is achieved because during $1/4$ of the utility period ($\pi/2$ rad), the load current ($i_L = i_\alpha$) is measured and stored in the DSP buffer. Thus, i_β in fact represents the quadrature current of the fictitious two-phase reference frame without any delay. In addition, if the utility frequency varies, the PLL system adjusts the time related to the $\pi/2$ rad delay that could cause any problem.

Furthermore, it is known that both the LPF and the PLL dynamic responses can interfere on the dynamic response of the PV-APF system. On the other hand, these interferences are not able enough to affect the PV-APF performance.

The PV-APF current reference i_c^* shown in Figure 5 is achieved as follows:

$$i_c^* = i_{SRF}K + i_{PV}. \quad (10)$$

As can be noted, the constant K that appears in (10) is used to control the amount of power processed by the PWM converter, in order that its rated current remains within the designed limits. This constant K is calculated by:

$$K = \frac{I_{SRFmax}}{I_{SRF}} = \frac{\sqrt{I_{inv}^2 - I_{PV}^2}}{I_{SRF}} = \frac{\sqrt{I_{inv}^2 - (i_{dc}/\sqrt{2})^2}}{I_{SRF}} \quad (11)$$

where I_{inv} is the nominal rms current of the VSI converter; I_{PV} is the actual PV array rms active current (i_{PV}) obtained from the dc-bus voltage controller; and I_{SRF} is the actual rms current obtained from SRF algorithm (i_{SRF}).

Thus, when $I_{SRF} \leq \sqrt{I_{inv}^2 - I_{PV}^2}$, $K = 1$, otherwise, $K < 1$ as obtained by (11), and, therefore, the amplitude of the current

i_{SRF} is reduced. Figure 6 presents the constant K , in function of the nominal rms SRF current (I_{SRF}).

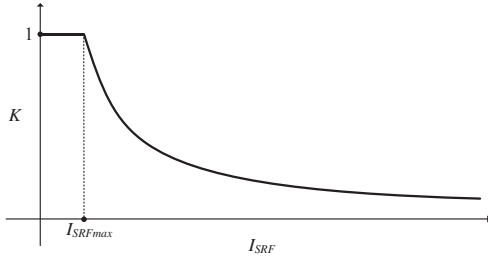


Fig. 6. Constant K used to control the power flow through the PV-APF system.

D. Current and dc-Bus Control Loops of the PV-APF System

The block diagram of the current controller used to control the 1F-B converter is shown in Figure 7, considering that the current reference i_c^* is achieved from the CRG presented in Figure 5. In addition, L_f and R_{L_f} are, respectively, the inductance and the resistance of the L-filter connected to the grid, and K_{PWM} represents the static gain of the PWM converter, which is calculated taking into account the peak value of the PWM triangular carrier [35].

As can be seen from (10), the compensating reference current i_c^* is not a continuous quantity. Thus, this leads to non-null errors in steady-state when conventional PI controller is employed. Thereby, a Proportional-Integral Multi-Resonant (PI-MR) controller [33], [34] is used to control the current synthesized by the 1F-B converter. This controller provides an infinite open loop gain at the resonant frequency (ω_o), which can result zero steady-state error [33].

The transfer function of the PI-MR controller is given by:

$$G_{PI-MR}(s) = k_{pi} + \frac{k_{ii}}{s} + \sum_{m=1}^n \frac{k_m s}{(s^2 + (m\omega_1)^2)} = G_{PI}(s) + \sum_{m=1}^n G_{MR(m)}(s) \quad (12)$$

where k_{pi} and k_{ii} represent, respectively, the proportional and integral gains of the current PI controller; k_m represents the resonant gains at a specific resonant frequency, ω_1 is the fundamental frequency, and $m = 1, 3, 5, \dots, n$. In this paper $n = 9$, meaning that the resonant terms are composed of the 1st, 3rd, 5th, 7th and 9th components. It is noted that the fundamental component ($m = 1$) is considered in (8), in order to compensate the load reactive component, as well as the active component injected into the grid, both at fundamental frequency.

In Figure 7 is also represented the dc-bus voltage controller. It is responsible to provide the signal i_{dc} to the CRG (Figure 5), in order to determine the amplitude of the active current that is injected into the grid. Thereby, the dc-bus control loop must present reduced bandwidth to avoid any distortions in reference current (i_c^*).

When the PV-APF system is working as shunt-APF only, the dc-bus voltage is maintained constant by draining active current from the electric grid. This current compensates the losses in the PV-APF system keeping dc-bus voltage constant.

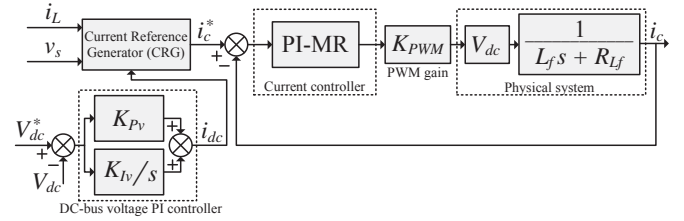


Fig. 7. Block diagram of the current control loop.

The proportional and integral dc-bus controller gains, k_{pv} and k_{iv} , shown in Figure 7, are determined using modeling and design procedures presented in [19].

E. PLL System

The single-phase PLL system implemented in this paper is shown in Figure 8. It uses a non-autonomous adaptive filter (AF) operating in conjunction with the $\alpha\beta$ -pPLL originating the AF- $\alpha\beta$ -pPLL scheme [20], [21]. In [21] it is presented the design requirements and procedures used for determining the PLL PI controller gains involving its stability analysis. In addition, extensive experimental tests confirm the good performance when this PLL scheme is submitted to utility disturbances, such as voltage harmonics, voltage sags/swells, phase-angle jumps and frequency variations.

The AF- $\alpha\beta$ -pPLL proportional (k_{ppll}) and integral (k_{ipll}) controller gains, as well as the AF gain $K_c = \mu/T_s$ are presented in Table II, where T_s is the DSP sampling time, μ is the adaptation step time, and A is the amplitude of the fundamental utility voltage, which is calculated based on the weights w_1 and w_2 of the AF, such that $A = \sqrt{w_1^2 + w_2^2}$ [20].

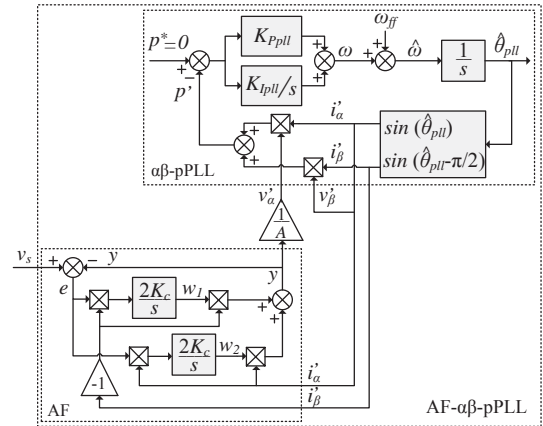


Fig. 8. Single-phase AF- $\alpha\beta$ -pPLL scheme.

III. IMPLEMENTATION OF THE PV-APF SYSTEM

Figure 1 shows the complete scheme of the PV-APF system. As can be seen, the SRF and PLL algorithms, the MPPT technique, the current and dc-bus voltage controllers, as well as the 1F-B converter of the PV-APF system were tested by means of numerical simulation, using the MATLAB/Simulink tools, and by experimentation. In addition, in order to perform the simulation tests as close as possible of the real system, all parts of the system were discretized, including the algorithms, data acquisition signals and controllers. Besides, the acquisition delays, normally introduced by the anti-aliasing filter, were taken into account,

as well as the dead-time of the switching devices. Table I summarizes the PV module parameters implemented in the simulations and experimentations, and Table II shows the parameters of the shunt-APF and the gains of the PI-MR, PI dc-bus, and PI PLL controllers. The procedure used for tuning all the PI controllers was based on the frequency response method via Bode diagrams [19]. This method can be employed when the phase margin and the 0dB gain crossover frequency are used as design specifications. In addition, the multi-resonant controller gains (k_m) presented in (12) are obtained in order to guarantee that each one of the multi-resonant crossover frequencies (ω_{cm}), related to $G_{MR(m)}$, are equal to the adopted crossover frequency (ω_{ci}) used in the PI current controller specification design, such that $\omega_{cm} = \omega_{ci}$.

The PV-APF system was experimentally tested based on the Digital Signal Processor (DSP) TMS320F28335 (Texas Instruments), which was used to implement the MPPT technique (Figure 4), the current reference generator (Figure 5), and the PLL algorithm (Figure 7). As can be seen, the nonlinear load used in the tests is composed of a full-bridge diode rectifier followed by RC load. The switching frequency of the PWM converter was set at 20 kHz. The full-bridge converter employs two IGBT modules (SK40GB 123 Semikron) with their proper drivers. Three current sensors model LEM LA 100-P are used to measure the PV array, load and converter currents. The input ac voltage and the dc-bus voltage (PV array voltage) are measured using two voltage sensors model LEM LV 25-P.

A. Simulation Results

Figure 9 shows the dynamic behavior of the PV-APF system taking into account three distinct operation modes (OPM), where the attenuation constant K , shown in Figure 6, is used to control the amount of power processed by the PWM converter.

Details related to the transitions from the OPM 1 to 2 and from the OPM 2 to 3 are shown in Figures 9 (a) and (b), respectively, where are shown the utility voltage (v_s), the utility current (i_s), the compensation current synthesized by the 1F-B converter (i_c) and the load current (i_L).

Initially, as shown in Figure 9 (a), from 19.95 to 20 s only load active power injection is carried out, while the reactive power compensation and harmonic current suppression are not taken into account (OPM 1). After that, from 20 to 20.25 s, both reactive power and harmonic currents are compensated in conjunction with the active power injection (OPM 2). Finally, as shown in Figure 9 (b), from 29.95 to 30 s the PV-APF system is operating in OPM 2. After that, from 30 to 30.25 s, the load apparent power (VA) related to the reactive power and harmonic components of the load is increased, occasioning the attenuation of the reference compensation current i_c^* (OPM 3). In Figure 9 (c) and (d) the ideal PV available power (P_{pv}^*), the power (P_{pv}) extracted from the PV arrays, the attenuation constant (K), the nominal rms current of the converter I_{inv} , the rms current of the converter I_c , the dc-bus voltage reference V_{dc}^* set by means of the MPPT technique, and the dc-bus voltage V_{dc} are shown considering the three OPMs. It is verified that there is no transition time between the OPMs 1 and 2. On the other

hand, the transition time between the OPMs 2 and 3 is around 200 ms. This transition time occurs due to the time spent to calculate the constant K , which depends on the calculation of the I_{PV} and I_{SRF} rms currents.

As can be noted, the attenuation constant (K) is forced to zero ($K = 0$) in OPM 1, while in the OPM 2 it is equal to one ($K = 1$) because $I_{SRF} \leq \sqrt{I_{inv}^2 - I_{PV}^2}$. In the OPM 3, since $I_{SRF} > \sqrt{I_{inv}^2 - I_{PV}^2}$, K is calculated according to (11) and its value is set between zero and one ($0 < K < 1$) as described in section II-C. As can be noted, in OPM 3, the most part of the active energy provided from the PV array is consumed by the load.

TABLE I
Standard Test Conditions (STC) of the SolarWorld Sunmodule Plus SW 245 PV Array

Maximum PV power	$P_{max} = 245\text{ W}$
Maximum power point voltage	$V_{mpp} = 30.8\text{ V}$
Maximum power point current	$I_{mpp} = 7.96\text{ A}$
Open circuit voltage	$V_{oc} = 37.5\text{ V}$
Short-circuit current	$I_{sc} = 8.49\text{ A}$

TABLE II
Parameters Adopted in the Simulation and Experimental Tests

Nominal utility rms voltage	$V_s = 127\text{ V}$
Nominal utility frequency	$f = 60\text{ Hz}$
Full-bridge converter nominal power	$S_{inv} = 2540\text{ VA}$
Nominal rms current of the full-bridge converter	$I_{inv} = 20\text{ A}$
Inductive filter	$L_f = 1.5\text{ mH}$
Inductive filter resistance	$R_{Lf} = 0.48\text{ }\Omega$
Load capacitance	$C = 940\text{ }\mu\text{F}$
Load resistance	$R = 30\text{ }\Omega$
Nominal load apparent power	$S_L = 1110\text{ VA}$
Load active power	$P_L = 870\text{ W}$
Load Displacement Power Factor	$\text{DPF} = 0.99$
Load Power Factor	$\text{PF} = 0.78$
Commutation inductance	$L_L = 1.2\text{ mH}$
MPP dc-bus voltage	$V_{dc} = 308\text{ V}$
dc-bus capacitor	$C_{dc} = 2115\text{ }\mu\text{F}$
Switching frequency	$f_{sw} = 20\text{ kHz}$
Sampling frequency A/D converter	$f_s = 60\text{ kHz}$
PWM gain	$K_{PWM} = 5.33 \times 10^{-4}$
Current PI-MR controller gains	$k_{pi} = 175.25; k_{I1} = 29727;$ $k_1 = 15700; k_3 = 15627;$ $k_5 = 15482; k_7 = 15265;$ $k_9 = 14975$
Crossover frequency (Current PI controller)	$\omega_{ci} = 15708\text{ rad/s}$
Phase-margin (Current PI controller)	$PM_i = 89.9^\circ$
dc-bus PI controller gains	$k_{pv} = 0.0996; k_{Iv} = 0.0902$
Crossover frequency (dc-bus controller)	$\omega_{cv} = 47.124\text{ rad/s}$
Phase-margin (dc-bus controller)	$PM_v = 88.9^\circ$
PLL PI controller gains	$k_{ppll} = 424.3; k_{Ipll} = 32234$
Crossover frequency (PLL PI controller)	$\omega_{cpll} = 430.874\text{ rad/s}$
Phase-margin (PLL PI controller)	$PM_{pll} = 80^\circ$
Adaptive filter gain	$K_c = 420$
Cut off frequency (SRF Controller) (2 nd order LPF Butterworth filter)	$f_c = 30\text{ Hz}$
P&O voltage step size	$\Delta v = 1\text{ V}$
P&O sampling time	$T_{SMPPT} = 0.5\text{ s}$

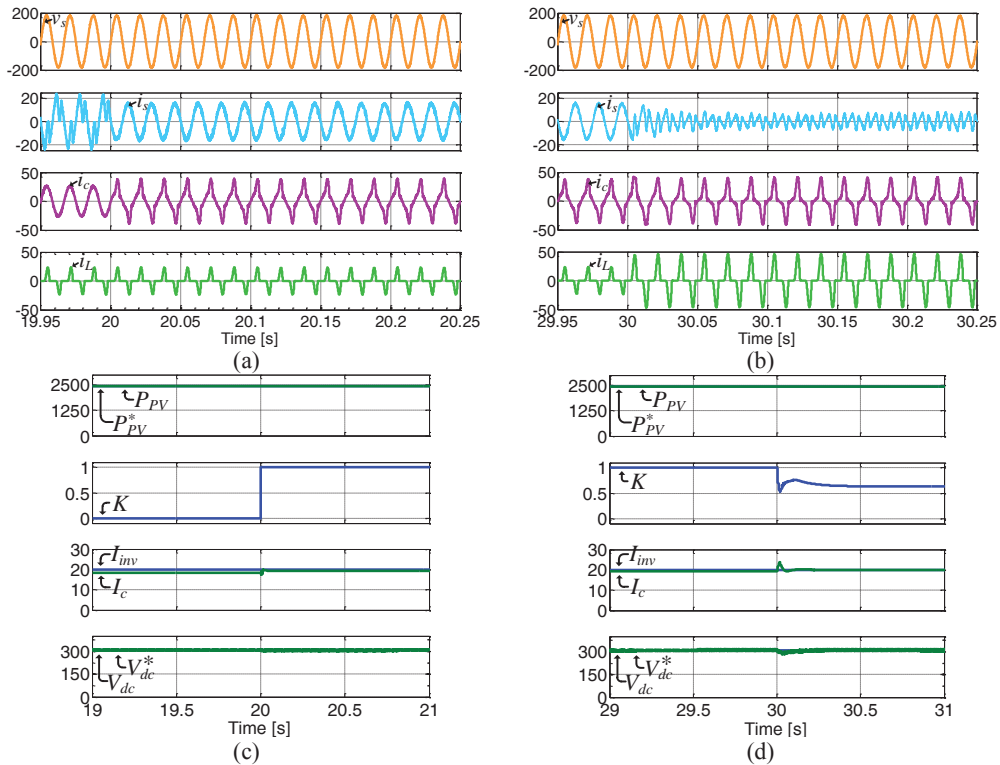


Fig. 9. Dynamic response for the OPMs 1, 2 and 3: (a) OPM 1 ($K = 0$) to OPM 2 ($K = 1$); (b) OPM 2 ($K = 1$) to OPM 3 ($0 < K < 1$); (c) details related to transition from OPM 1 to OPM 2; (d) details related to transition from OPM 2 to OPM 3.

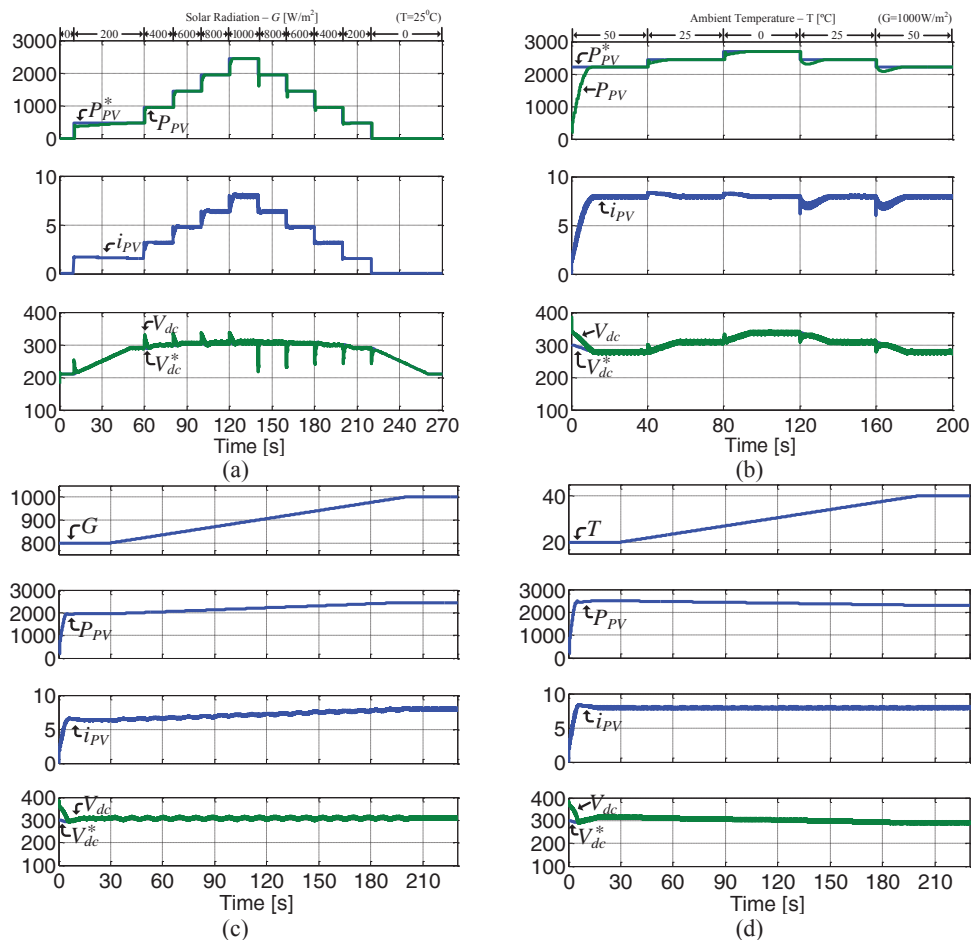


Fig. 10. MPPT dynamic during step and linear variations in the atmospheric conditions: (a) step variation in G ; (b) step variation in T ; (c) linear variation in G ; (d) linear variation in T .

Taking into account atmospheric condition changes (step and linear variations), the behavior of the PV-APF system is evaluated based on the quantities presented in Figure 10, where are shown the ideal available PV array power (P_{pv}^*), the power extracted from the PV array (P_{pv}), the PV array current (i_{pv}), the dc-bus voltage reference set by the MPPT algorithm (V_{dc}^*), the dc-bus voltage (V_{dc}), the solar radiation (G), and the ambient temperature (T). In Figure 10 (a) and (b) results related to step variations in G and T , respectively, are shown, while results related to linear variation are shown in Figure 10 (c) and (d). It can be noted that the MPP is tracked for all ranges of temperature and solar radiation. Besides, the amplitude of the dc-bus voltage is higher than 210 V, as required in the design specifications.

B. Experimental Results

The static behavior of the PV-APF system is evaluated by means of the experimental results shown in Figure 11. It was considered four different cases related to the PV-APF system operation, which are described as follows: i. active power injection for the nonlinear load disconnected (case 1); ii. load reactive power compensation and harmonic current suppression (active power filtering), and utility grid active power injection (case 2); iii. active power filtering and both utility grid and load active power injection (case 3); and iv. active power filtering only (case 4). The following quantities are shown: voltage source (v_s), source current (i_s), compensation current (i_c), and load current (i_L).

In case 1, all the active power produced by the PV array (P_{pv}) is injected into the grid, because the load is disconnected. As can be noted in Figure 11 (a), the sinusoidal source current i_s is in opposite phase with the utility voltage v_s ; in case 2, P_{pv} is higher than the load active power P_L .

Thus, P_{pv} is provided to both utility grid and the load, as can be seen in Figure 11 (b); in case 3, P_{pv} is lower than P_L . In this case, P_{pv} is totally provided to the load as shown in Figure 11 (c); and finally, Figure 11 (d) presents the results for the case 4, where P_{pv} is null. In this case, the PV-APF system performs the active power filtering only. It is verified that the source current is in phase with utility voltage.

Table III presents the total harmonic distortion (THD) related to the compensated source current i_s considering the four operation modes of the PV-APF system. As can be observed, the THD of the source current was reduced in all presented cases (1, 2, 3, and 4), mainly in the case 1 ($P_{pv} > 0$ and $P_L = 0$), where the PV-APF system is only injecting active power into the grid ($THD_{i_s} < 5\%$) [36].

The dynamic behavior of the PV-APF system is evaluated by means of the experimental results shown in Figure 12. Figure 12 (a) shows the MPP power (P_{pv}) extracted from the PV array, the PV array current i_{pv} , and the dc-bus voltage V_{dc} , when a PV-array disconnection occurs at 0.7 s. As can be noted, from 0 to 0.7 s, the dc-bus voltage reference V_{dc}^* is set by means of the MPPT-P&O algorithm. After that, P_{pv} and i_{pv} fall to zero and the PV-APF system remains operating as APF and the dc-bus is set at 210 V.

Figure 12 (b) and (c) shows the dynamic behavior of the PV-APF system when the nonlinear load step is suddenly applied. All the time, the PV-APF system shares the active energy produced by the PV array between the utility grid and the load. After the transient, it can be observed that the peak amplitude of the PV-APF system (i_c) increases and the source current (i_s) decreases, once the load current was increased. In this case, it is noted that the additional energy absorbed by the load was provided by the PV-APF system.

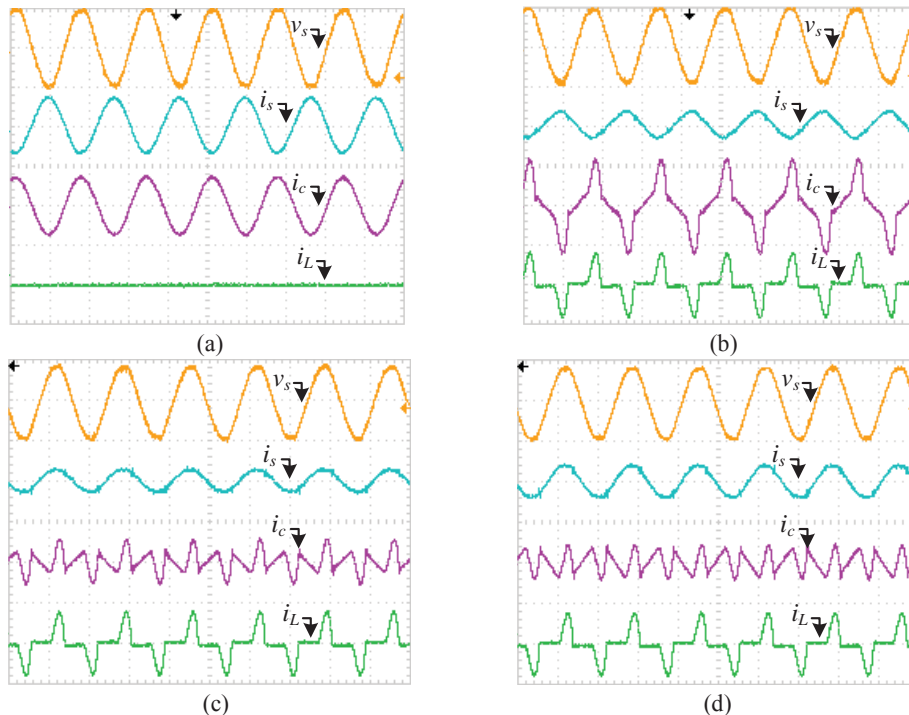


Fig. 11. Utility voltage v_s (200V/div, 10ms/div) and currents i_s , i_c , and i_L (30A/div, 10ms/div) for the PV-APF system: (a) case 1 ($P_{pv} = 2000$ W; $P_s = -1820$ W and $P_L = 0$ W); (b) case 2 ($P_{pv} = 2000$ W; $P_s = -1030$ W and $P_L = 870$ W); (c) case 3 ($P_{pv} = 300$ W; $P_s = 690$ W and $P_L = 870$ W); and (d) case 4 ($P_{pv} = 0$ W; $P_s = 980$ W and $P_L = 870$ W).

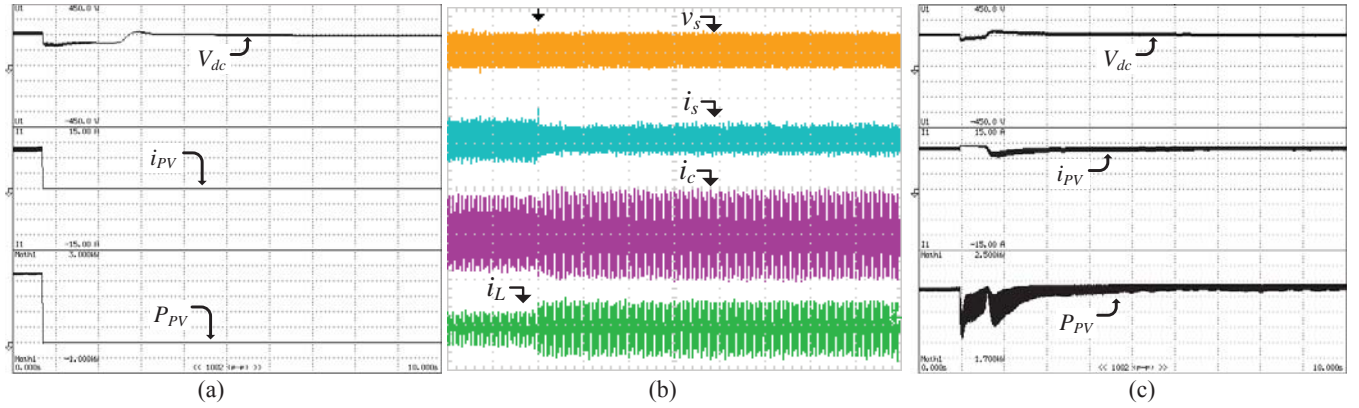


Fig. 12. PV-APF system dynamic responses (1 s/div): (a) PV array quantities, i_{pv} (3.75 A/div), P_{pv} (500 W/div) and V_{dc} (112.5 V/div) for PV array disconnection; (b) utility voltage v_s (500 V/div), currents i_s , i_c , and i_L (40 A/div) for load step; (c) PV array quantities: V_{dc} (112.5 V/div), i_{pv} (3.75 A/div), and P_{pv} (100 W/div) for load step.

TABLE III
THD of the Source and Load Currents for the Load Composed of a Full-Bridge Diode Rectifier Followed by RC Load (Experimental Results)

Cases 1, 2, 3 and 4.	(THD %)	
	i_L	i_s
1. Active power injection, without nonlinear load connected ($P_{pv} > 0$ and $P_L = 0$)	----	1.8
2. Active power injection with reactive and harmonic compensation ($P_{pv} > P_L$)	60	7.3
3. Active power injection with reactive and harmonic compensation ($P_{pv} < P_L$)	60	8.0
4. Reactive and harmonic compensation, with nonlinear load connected ($P_{pv} = 0$)	60	5.9

IV. CONCLUSION

This work presented a single-phase grid-tied PV system implementation with active power line filtering capability. An alternative current reference generator algorithm was proposed to perform active power injection into the grid, as well as load harmonic suppression and reactive power compensation. The PV-APF system was connected to the grid by means of a 1F-B converter, while the PV array was connected to the dc-bus without the step-up dc/dc converter use. Thus, the MPPT-P&O technique acted directly on the 1F-B converter. In addition, it was proposed a calculation algorithm, used to limit the amount of the power processed by the 1F-B converter, when the PV-APF is injecting power into the grid and, simultaneously, operating as APF.

By means of simulation and experimental results, it was verified the static and dynamic behaviors of the PV-APF system, where good performance and effectiveness were achieved.

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