

# AC FIVE-PHASE DRIVE SYSTEMS BASED ON CASCADE CONVERTERS AND OPEN-END WINDING FIVE PHASE MACHINE

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**Abstract** - This paper presents two AC machine drive systems based on three-phase to five-phase AC-AC converters and open-end winding five-phase machine. The drive systems are suitable for applications in which high power, performance and reliability are required using low power and voltage switches and low DC-link capacitor voltages. The configuration I employs an input transformer with two secondary taps at the grid side, two three-phase three-leg converters and one ten-leg converter (totaling sixteen legs). The configuration II employs a low-power series transformer at the grid side, two three-phase three-leg converters, and one ten-leg converter. Both configurations permit to reduce the power and voltage ratings of power switches and also the DC-link capacitor size. The paper presents the comprehensive models of the proposed systems, modulation strategies and a general comparison with the conventional configuration. Simulated and experimental results are presented.

**Keywords** – AC drive, Cascade converter, Multilevel converter, Open-end winding machine

## I. INTRODUCTION

Electrical motors are responsible for the majority of the electrical power consumed worldwide. For instance, it is believed that in the industrial sector they represent about  $\frac{2}{3}$  of total electrical power consumption [1]. Moreover, since the 1980's that AC drives have been replacing DC drives in most of industrial applications [2], [3]. In this way, most of modern applications use AC electrical machinery [4]. The most popular AC drive system is based on an AC-DC-AC power converter with a front-end diode bridge rectifier followed by a PWM voltage source inverter (VSI) and a three-phase electrical machine [2]. In order to improve the power quality at the grid side, the traditional solution is the DC-link with double-ended PWM bridges described in [5] and shown in Figure 1.

Traditionally, AC electrical machines have consolidated as three-phase. The main reason for such number of phases is the

three-phase power system, because previously to the modern power electronics converters [2] the AC machines, specially induction ones, were primarily used directly connected to the three-phase power supply. However, modern variable speed AC drives [6] are fed by power converters, therefore any number of phases may be used [7]. From the converter point of view, a multiphase drive is a natural way to increase the total power of the drive system without increasing the rated conditions of each converter power switch. Moreover, multiphase machines have several inherent advantages if compared to three-phase ones. For instance, multiphase induction machines have lower pulsating torque, reduced acoustic noise and losses, lower space-harmonic content, and greater fault tolerance capability [7–17].

Another solution to achieve medium to high power drive systems, instead of using power switches with high voltage and high current characteristics [18], [19] is the use of multilevel converters [20], mainly neutral point clamped configurations and cascade configurations [21–24]. Another possible multilevel configuration in AC drive is the open windings configurations, first reported in [25] and widely explored since then [26–31]. The so called open-end winding configurations allow for multilevel voltages at the machine windings, higher power levels with smaller rated power converters, and reduced losses [32].

The multilevel converters reduces the voltage across each power switch while the multiphase system reduces the current and voltage. Hence, several research effort has been dedicated to such configurations [33], [34]. For instance, in [29] is shown a space vector PWM for the dual-inverter five-phase open-end winding topology.

The conventional five-phase AC drive system connected to the three-phase power grid is shown in Figure 2. It comprises a DC-link with double-ended PWM bridges. In this paper are presented two AC five-phase drive systems based on cascade converters and open-end winding five phase machines in a three-phase to five-phase power conversion configuration, shown in Figures 3 and 4. The proposed configurations allow for reduced rated power and voltage in the power switches and the DC-link capacitor. Moreover, because of the multilevel characteristics they present lower harmonic distortions and provide several extra degrees of freedom which allow for a greater fault tolerance if compared to the conventional

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configuration, therefore allowing for greater reliability. The term reliability is usually used to express the capability of a system to stay functional [35]. A certain system is said to have high availability if it has a high time between failures and a low time to repair [35]. The configuration *I* (Conf. *I*), shown in Figure 3, is composed of an input transformer with two secondary taps at the grid side, two three-phase three-leg converters (converters  $A_g$  and  $B_g$ ), a ten-leg converter (converters  $A_s$  and  $B_s$ ) and an open-end winding five-phase machine. This configuration requires the two secondary windings in order to allow for two separated DC-link voltages (multilevel cascade converters at the grid side) and to avoid zero sequence (circulating) currents between the open-end winding at the machine side and the cascade converters at the grid side. The configuration *II* (Conf. *II*), shown in Figure 4 is composed of a low-power series transformer at the grid side, two three-phase three-leg converters (converters  $A_g$  and  $B_g$ ), a ten-leg converter (converters  $A_s$  and  $B_s$ ), and an open-end winding five-phase machine. This configuration uses a single winding secondary transformer, unlike Conf. *I*, and still allows for separated DC-link voltages and zero circulating currents. Besides, the series transformer turns ratio can be properly chosen in order to increase the number of voltages level at the input grid converters. On the other hand, the Conf. *II* has no isolation from the power mains which is the case for Conf. *I*. A comprehensive analysis of the power converters model, *PWM* strategy and control is presented. Simulated and experimental results are carried out in order to verify the presented analysis.

## II. SYSTEM MODEL

### A. Machine side converter

The same model stands for both configurations (Figures 3 and 4). Moreover, this paper is focused in the converter analysis, therefore a specific AC machine is not described. Instead a general *RLE* five-phase load (resistive-inductive with an internal voltage) is used in order to emulate the machine voltage/current operation conditions. Such simplification does not compromise the analysis since the presented configurations can be used for any AC machine drive. Therefore, the phase voltages in Figures 3 and 4 can be written as

$$v_{sj} = v_{saj0_a} - v_{0_b0_a} - v_{sbj0_b} = e_{sj} + l_s \frac{di_{sj}}{dt} + r_s i_{sj} \quad (1)$$

with  $j = 1, 2, 3, 4, 5$  and where  $v_{saj0_a}$  and  $v_{sbj0_b}$  are the pole voltages and  $v_{0_b0_a}$  is the voltage between the DC-link midpoints  $0_b$  and  $0_a$ . From (1) and considering balanced symmetric machine, the voltage  $v_{0_b0_a}$  can be written as

$$v_{0_b0_a} = \frac{1}{5} \sum_{j=1}^5 v_{saj0_a} - \frac{1}{5} \sum_{j=1}^5 v_{sbj0_b}. \quad (2)$$

Then, the machine voltages become

$$v_{sj} = v_{saj0_a} - v_{sbj0_b} - \frac{1}{5} \sum_{j=1}^5 v_{saj0_a} + \frac{1}{5} \sum_{j=1}^5 v_{sbj0_b}. \quad (3)$$

For instance, if  $v_{C_a} = v_{C_b}$ , the phase voltage in (3) has seventeen possible voltage levels, while the phase voltage in

the conventional configuration in Figure 2 has nine possible levels only. If the DC-link voltages are different, then the possible number of levels in the phase voltage increases significantly, for example, if  $v_{C_b} = \frac{1}{2}v_{C_a}$  the phase voltage can take twenty five possible voltage levels; if  $v_{C_b} = \frac{2}{3}v_{C_a}$  this level number is increased to thirty nine.

### B. Grid side converter

#### Conf. *I*

Considering the equivalent circuit of Figure 6, the grid side converter model for Conf. *I* is given by

$$v_{gnk} = v_{gnk0_n} - v_{gn0_n} = e_{gnk} - l_g \frac{di_{gnk}}{dt} - r_g i_{gnk}, \quad (4)$$

then

$$v_{gn0_n} = \frac{1}{3} \sum_{k=1}^3 v_{gnk0_n} \quad (5)$$

where  $k = 1, 2, 3, n = a, b$ .

Each secondary phase voltage has five possible voltage levels.

#### Conf. *II*

Considering the equivalent circuit of Figure 7, the grid side converter model for Conf. *II* is given by

$$v_{gk} = v_{gak0_a} + e_{gbk} - v_{g0_a} = e_{gak} - l_g \frac{di_{gk}}{dt} - r_g i_{gk} \quad (6)$$

$$v_{gbk} = v_{gbk0_b} - v_{gb0_b} = e'_{gbk} - l'_g \frac{di_{gbk}}{dt} - r'_g i_{gbk} \quad (7)$$

where  $k = 1, 2, 3$  and

$$v_{g0_a} = \frac{1}{3} \sum_{k=1}^3 v_{gak0_a} \quad (8)$$

$$v_{gb0_b} = \frac{1}{3} \sum_{k=1}^3 v_{gbk0_b} \quad (9)$$

with  $e_{gbk} = N e'_{gbk}$  ( $N$  is the turns ratio of the ideal transformer).

The series transformer allows for a multilevel voltage at the grid side which can be properly chosen by the transformer turns ratio.

## III. PWM: MODULATING SIGNALS DEFINITION

The gating signals are obtained by comparing the reference pole voltages on the grid side  $v_{gnk0_n}^*$  and on the machine side  $v_{snj0_n}^*$  (where  $n = a, b; k = 1, \dots, 3; j = 1, \dots, 5$ ) to one or more high frequency triangular carrier signals. These reference pole voltages are the modulating signals and they must be defined from the phase voltages reference (on the grid and machine sides), which are in turn defined by the active and reactive power control from the grid and the machine control system, as will be shown in Section V. Once the phase voltages reference are defined by the control system (see Section V) the modulating signals for the machine side converters and grid side converters can be defined as follows.

### A. Machine side converter

The simplified machine side converter equivalent circuit is shown in Figure 5. It is required to calculate ten pole voltages

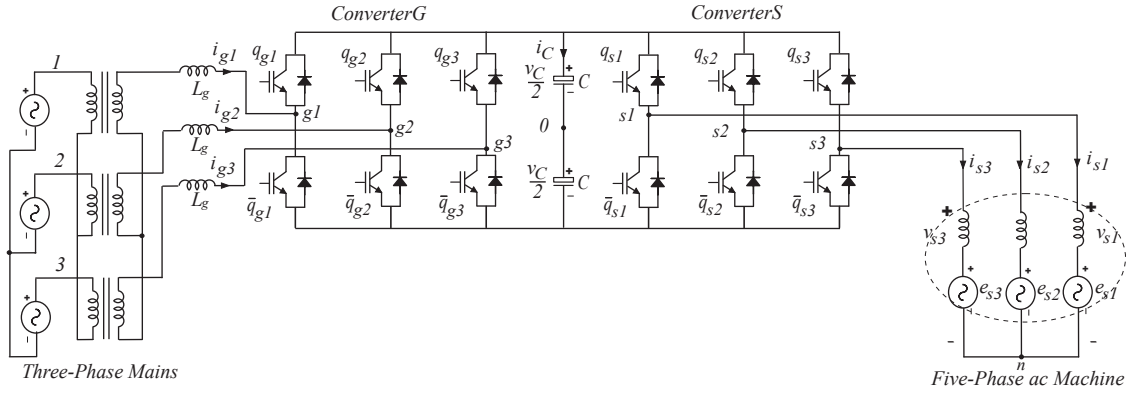


Fig. 1. Conventional three-phase AC drive system (C-3ph).

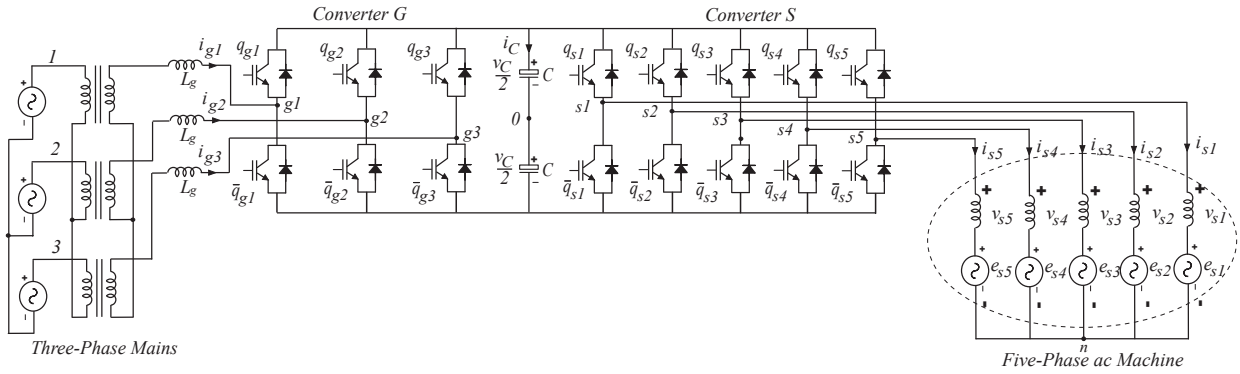


Fig. 2. Conventional five-phase AC drive system (C-5ph).

$v_{snj0n}^*$ ,  $j = 1, \dots, 5$  and  $n = a, b$ . However, only four voltages are necessary to control the system (four among  $v_{sj}$ ,  $j = 1, \dots, 5$ ). Then, six auxiliary variables, named  $v_{0b0a}^*$ ,  $v_{sx1}^*$ ,  $v_{sx2}^*$ ,  $v_{sx3}^*$ ,  $v_{sx4}^*$ , and  $v_{sx5}^*$ , are defined.

In order to simplify the auxiliary variables calculation, we determine first  $v_{0b0a}^*$ . Introducing variables  $v_{srj}^*$ , as shown in the modified equivalent circuit in Figure 5, that is,

$$v_{srj}^* = v_{saj0a}^* - v_{sbj0b}^*. \quad (10)$$

The reference machine voltages  $v_{sj}^*$  can be expressed by

$$v_{sj}^* = v_{srj}^* - v_{0b0a}^*. \quad (11)$$

Consequently, it follows that

$$v_{srj}^* = v_{sj}^* + v_{0b0a}^*. \quad (12)$$

Voltage  $v_{0b0a}^*$  must be chosen such that

$$v_{0b0a}^* \min \leq v_{0b0a}^* \leq v_{0b0a}^* \max \quad (13)$$

$$v_{0b0a}^* \min = -v_C^* - \min\{v_{s1}^*, v_{s2}^*, v_{s3}^*, v_{s4}^*, v_{s5}^*\} \quad (14)$$

$$v_{0b0a}^* \max = v_C^* - \max\{v_{s1}^*, v_{s2}^*, v_{s3}^*, v_{s4}^*, v_{s5}^*\} \quad (15)$$

where  $v_{Ca}^*$  and  $v_{Cb}^*$  are the reference DC-link voltages of converters  $A_s$  and  $B_s$ , respectively; and  $v_C^* = (v_{Ca}^* + v_{Cb}^*)/2$ . Given  $v_{0b0a}^*$ , voltages  $v_{srj}^*$  are determined from (12).

The auxiliary variables  $v_{sxj}^*$  are expressed by

$$v_{sxj}^* = \frac{1}{2}(v_{saj0a}^* + v_{sbj0b}^*). \quad (16)$$

Then, the pole voltages are given by

$$v_{saj0a}^* = v_{srj}^*/2 + v_{sxj}^*; \quad v_{sbj0b}^* = -v_{srj}^*/2 + v_{sxj}^*. \quad (17)$$

Voltage  $v_{sxj}^*$  must be chosen respecting the limits

$$v_{sxj}^* \min \leq v_{sxj}^* \leq v_{sxj}^* \max \quad (18)$$

$$v_{sxj}^* \min = \max\{v_{saxj}^* \min, v_{sxbj}^* \min\} \quad (19)$$

$$v_{sxj}^* \max = \min\{v_{saxj}^* \max, v_{sxbj}^* \max\} \quad (20)$$

where

$$v_{saxj}^* \min = -v_{Ca}^*/2 - v_{srj}^*/2 \quad (21)$$

$$v_{sxbj}^* \min = -v_{Cb}^*/2 + v_{srj}^*/2 \quad (22)$$

$$v_{saxj}^* \max = v_{Ca}^*/2 - v_{srj}^*/2 \quad (23)$$

$$v_{sxbj}^* \max = v_{Cb}^*/2 + v_{srj}^*/2. \quad (24)$$

The normalized choice of the auxiliaries variables satisfying their limits, can be provided introducing normalization variables  $\mu_{sxj}^*$  ( $0 \leq \mu_{sxj}^* \leq 1$ ) for the auxiliaries variables  $v_{sxj}^*$  and  $\mu_{0b0a}^*$  ( $0 \leq \mu_{0b0a}^* \leq 1$ ) for the auxiliary variable  $v_{0b0a}^*$ . Therefore, the auxiliary variable  $v_{0b0a}^*$  can be written as

$$v_{0b0a}^* = \mu_{0b0a}^* v_{0b0a}^* \max + (1 - \mu_{0b0a}^*) v_{0b0a}^* \min, \quad (25)$$

while  $v_{sxj}^*$  are written as

$$v_{sxj}^* = \mu_{sxj}^* v_{sxj}^* \max + (1 - \mu_{sxj}^*) v_{sxj}^* \min. \quad (26)$$

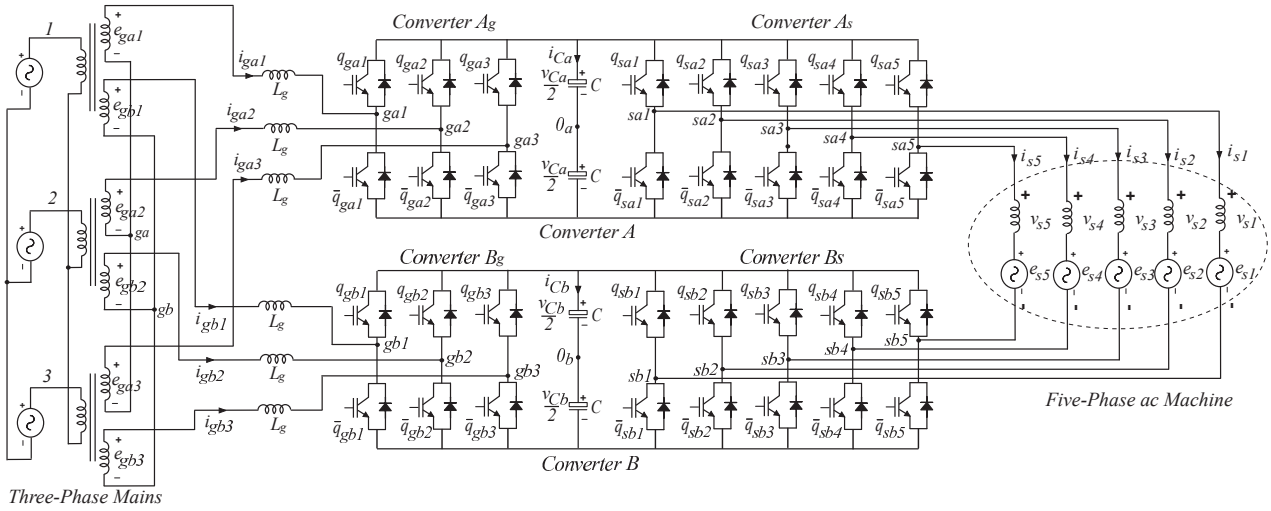


Fig. 3. Open-end winding five-phase machine AC drive system (Conf. I).

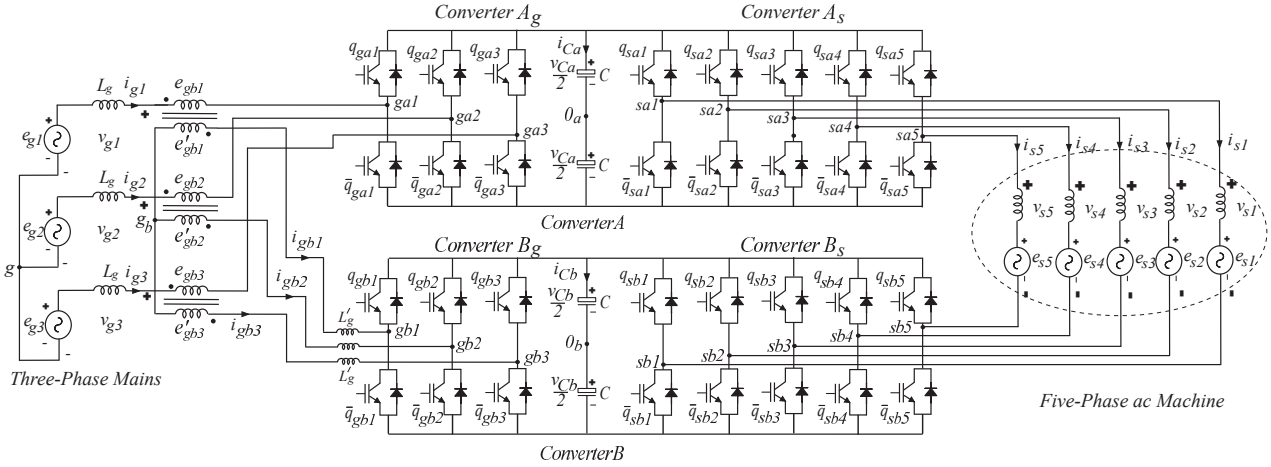


Fig. 4. Open-end winding five-phase machine AC drive system with series transformer (Conf. II).

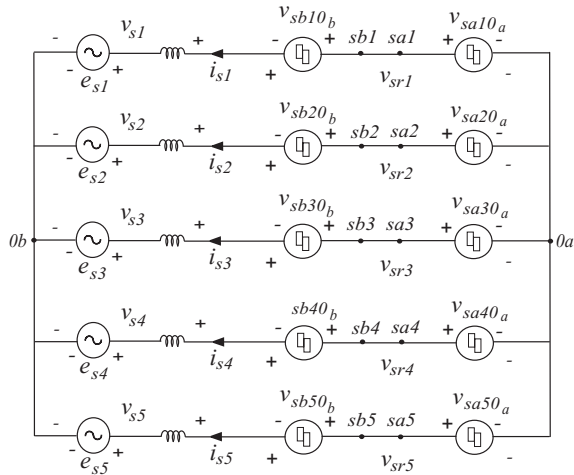


Fig. 5. Machine side equivalent circuit for both Conf. I and Conf. II.

The calculation of the reference pole voltages from the machine reference phase voltages  $v_{sj}^*$ ,  $j = 1, \dots, 5$  is given

by the following algorithm:

- Step 1: a) determine  $v_{0b0a}^*$  min and  $v_{0b0a}^*$  max from (14) and (15); b) choose  $\mu_{0b0a}^*$ ; c) determine  $v_{0b0a}^*$  from (25), and d) determine  $v_{sr1}^*$ ,  $v_{sr2}^*$ ,  $v_{sr3}^*$ ,  $v_{sr4}^*$ , and  $v_{sr5}^*$  from (12).

- Step 2: a) determine  $v_{sxj}^*$  min and  $v_{sxj}^*$  max from (19) and (20); b) choose  $\mu_{sxj}^*$ ; c) determine  $v_{sxj}^*$  from (26); and d) determine the ten pole voltages  $v_{sa10a}^*$  to  $v_{sb50b}^*$  from (17).

#### B. Grid side converter - Conf. I

The equivalent circuits are shown in Figure 6. It can be written that

$$v_{gnk0n}^* = v_{gnk}^* + v_{gn0n}^* \quad (27)$$

where  $n = a, b$  and  $k = 1, 2, 3$ . Voltage  $v_{gn0n}^*$  must be chosen such that

$$v_{gn0n}^* \min \leq v_{gn0n}^* \leq v_{gn0n}^* \max \quad (28)$$

$$v_{gn0n}^* \min = -v_{Cn}^*/2 - \min\{v_{gn1}^*, v_{gn2}^*, v_{gn3}^*\} \quad (29)$$

$$v_{gn0n}^* \max = v_{Cn}^*/2 - \max\{v_{gn1}^*, v_{gn2}^*, v_{gn3}^*\}. \quad (30)$$

Introducing  $\mu_{gn0n}^*$  ( $0 \leq \mu_{gn0n}^* \leq 1$ ), the auxiliary variable  $v_{gn0n}^*$  can be written as

$$v_{gn0n}^* = \mu_{gn0n}^* v_{gn0n}^* \max + (1 - \mu_{gn0n}^*) v_{gn0n}^* \min. \quad (31)$$

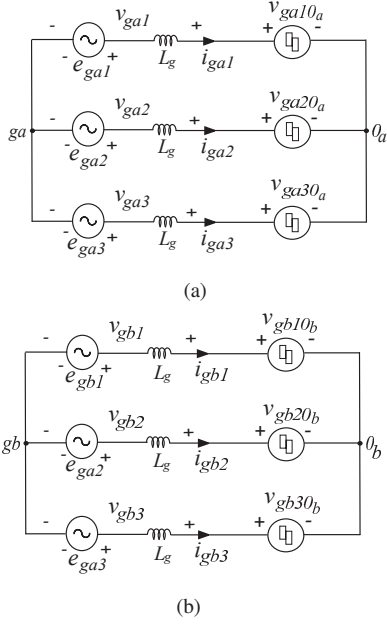


Fig. 6. Grid side converter equivalent circuits for Conf. I: (a) Converter  $A_g$  model; and (b) Converter  $B_g$  model.

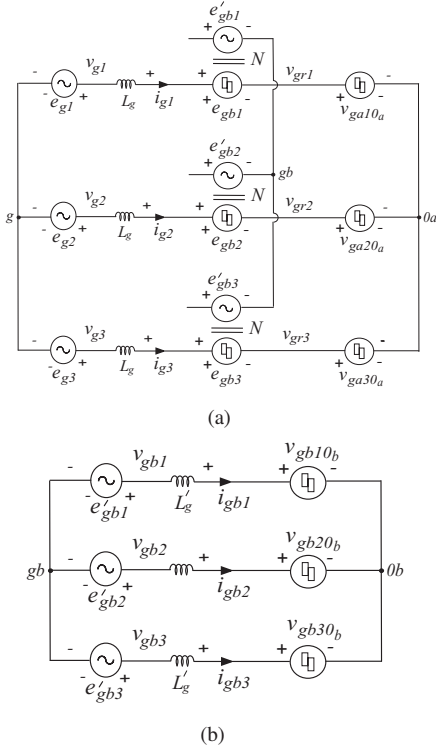


Fig. 7. Grid side converter equivalent circuits for Conf. II: (a) Complete model; and (b) Converter  $B$  model.

Hence, the pole voltages  $v_{gk0_n}^*$  can be determined from (31) and (27).

### C. Grid side converter - Conf. II

The equivalent circuits are shown in Figure 7. It can be written that

$$v_{grk}^* = v_{gak0_a}^* + e_{gbk}^* = v_{gk}^* + v_{g0_a}^* \quad (32)$$

where  $k = 1, 2, 3$ . Voltage  $v_{g0_a}^*$  must be chosen such that

$$v_{g0_a}^* \min \leq v_{g0_a}^* \leq v_{g0_a}^* \max \quad (33)$$

$$v_{g0_a}^* \min = -v_C^* - \min\{v_{g1}^*, v_{g2}^*, v_{g3}^*\} \quad (34)$$

$$v_{g0_a}^* \max = v_C^* - \max\{v_{g1}^*, v_{g2}^*, v_{g3}^*\} \quad (35)$$

where

$$v_C^* = v_{C_a}^*/2 + v_{C_b}^*N/\sqrt{3}. \quad (36)$$

The pole voltage  $v_{gak0_a}^*$  in (32) is limited to  $\pm \frac{v_{C_a}^*}{2}$ , besides the voltage  $e_{gbk}^*$  is limited to  $\pm \frac{v_{C_b}^*}{\sqrt{3}}$  and  $e_{gbk}^* = Ne_{gbk}'^*$  (where  $N$  is the transformer turn ratio), therefore  $v_C^*$  in (36) is the limit for  $v_{gak0_a}^* + e_{gbk}^*$ .

Introducing  $\mu_{g0_a}^*$  ( $0 \leq \mu_{g0_a}^* \leq 1$ ), the auxiliary variable  $v_{g0_a}^*$  can be written as

$$v_{g0_a}^* = \mu_{g0_a}^* v_{g0_a}^* \max + (1 - \mu_{g0_a}^*) v_{g0_a}^* \min. \quad (37)$$

From (37) and (32) the voltages  $v_{grk}^*$ ,  $k = 1, 2, 3$  are determined.

Introducing auxiliary variables  $v_{gk}^*$  expressed by

$$v_{gk}^* = \frac{1}{2}(v_{gak0_a}^* - e_{gbk}^*). \quad (38)$$

The pole voltages are given by

$$v_{gak0_a}^* = v_{grk}^*/2 + v_{gk}^*; \quad e_{gbk}^* = v_{grk}^*/2 - v_{gk}^*. \quad (39)$$

Voltage  $v_{gk}^*$  must be chosen respecting the limits

$$v_{gk}^* \min \leq v_{gk}^* \leq v_{gk}^* \max \quad (40)$$

$$v_{gk}^* \min = \max\{v_{gak0_a}^* \min, e_{gbk}^* \min\} \quad (41)$$

$$v_{gk}^* \max = \min\{v_{gak0_a}^* \max, e_{gbk}^* \max\} \quad (42)$$

where

$$e_{gbk}^* \min = -v_{C_b}^*N/\sqrt{3} + v_{grk}^*/2 \quad (43)$$

$$v_{gak0_a}^* \min = -v_{C_a}^*/2 - v_{grk}^*/2 \quad (44)$$

$$e_{gbk}^* \max = v_{C_b}^*N/\sqrt{3} + v_{grk}^*/2 \quad (45)$$

$$v_{gak0_a}^* \max = v_{C_a}^*/2 - v_{grk}^*/2. \quad (46)$$

Introducing  $\mu_{gk}^*$  ( $0 \leq \mu_{gk}^* \leq 1$ ), the auxiliaries variables  $v_{gk}^*$  can be determined by

$$v_{gk}^* = \mu_{gk}^* v_{gk}^* \max + (1 - \mu_{gk}^*) v_{gk}^* \min. \quad (47)$$

Therefore, the pole voltages  $v_{gak0_a}^*$  and  $e_{gbk}^*$  are calculated from from (47) and (39).

The pole voltages  $v_{gbk0_b}^*$  are given by

$$v_{gbk0_b}^* = e_{gbk}'^* + v_{gb0_b}^*. \quad (48)$$

The auxiliary voltage  $v_{gb0_b}^*$  is limited by

$$v_{gb0_b}^* \min \leq v_{gb0_b}^* \leq v_{gb0_b}^* \max \quad (49)$$

$$v_{gb0_b}^* \min = -v_{C_b}^*/2 - \min\{e_{gb1}'^*, e_{gb2}'^*, e_{gb3}'^*\} \quad (50)$$

$$v_{gb0_b}^* \max = v_{C_b}^*/2 - \max\{e_{gb1}'^*, e_{gb2}'^*, e_{gb3}'^*\} \quad (51)$$

where  $e_{gbk}'^* = Ne_{gbk}^*$  and  $N$  is the transformer turn ratio. Introducing  $\mu_{gb0_b}^*$  ( $0 \leq \mu_{gb0_b}^* \leq 1$ ) the auxiliary variable  $v_{gb0_b}^*$  can be determined as

$$v_{gb0_b}^* = \mu_{gb0_b}^* v_{gb0_b}^* \max + (1 - \mu_{gb0_b}^*) v_{gb0_b}^* \min. \quad (52)$$

Hence, the pole voltages  $v_{gbk0_b}^*$  are calculated from (52) and (48).

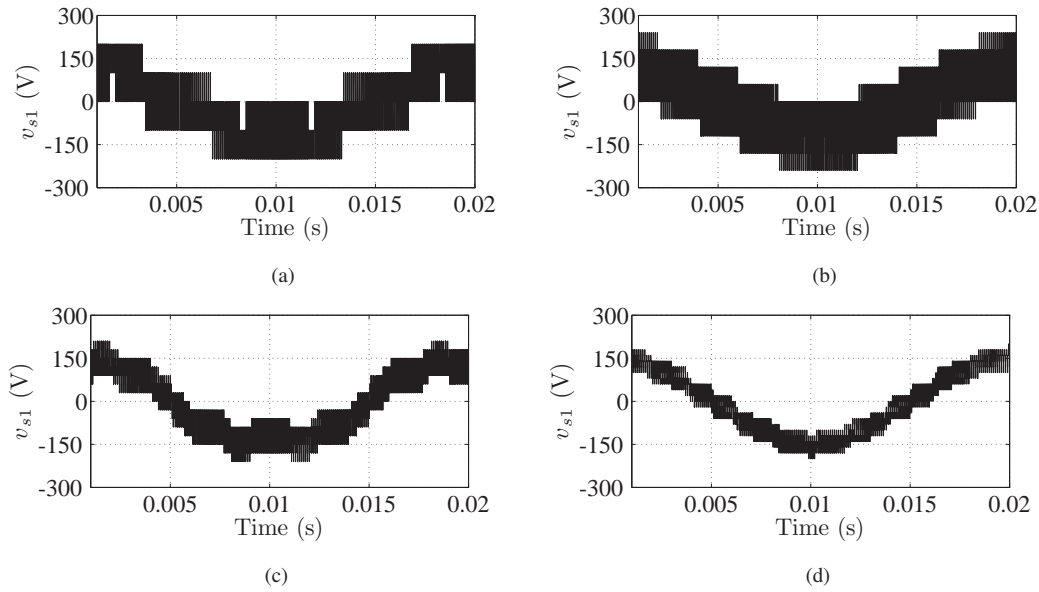


Fig. 8. Machine phase voltage  $v_{s1}$  for (a) The conventional three-phase AC drive; (b) The conventional five-phase AC drive; (c) The five-phase AC drive in open-end winding configuration using PD-PWM and same DC-link voltages; and (d) The five-phase AC drive in open-end winding configuration using PD-PWM and  $v_{Ca} = \frac{4}{3}v_C$  and  $v_{Cb} = \frac{2}{3}v_C$ .

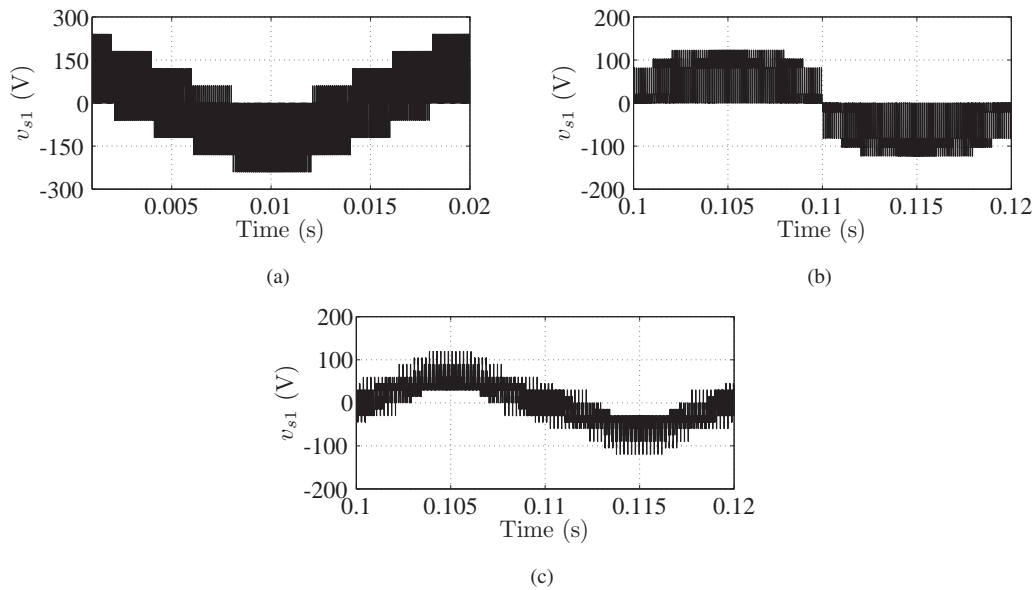


Fig. 9. Machine phase voltage  $v_{s1}$  for (a) The conventional five-phase AC drive; (b) The five-phase AC drive in open-end winding configuration and a single triangular carrier for both converters; and (c) The five-phase AC drive in open-end winding configuration using PS-PWM.

#### IV. MULTICARRIER PWM STRATEGIES

The gating signals are obtained by comparing the reference pole voltages on the grid side  $v_{gmk0n}^*$  and on the machine side  $v_{snj0n}^*$  (where  $n = a, b$ ;  $k = 1, \dots, 3$ ; and  $j = 1, \dots, 5$ ) to one or more high frequencies triangular carrier signals. In this paper are explored two multi-carrier strategies as in [36]: A Phase Shifted Carrier PWM (PS-PWM); and a Phase Disposition Carrier PWM (PD-PWM).

In the PS-PWM approach there are two high frequencies triangular carriers phase shifted by  $90^\circ$  as shown in Figure 10. The reference pole voltages associated to the upper DC-link

converters and to the lower DC-link converters in Figures 3 and 4 are compared to each one of the high frequency carriers, respectively.

In the PD-PWM approach the triangular carriers are in phase, however with different offsets. It is considered two distinct cases:

1. Same DC-link converters voltages ( $v_{Ca} = v_{Cb} = v_C$ ): In such case the PD-PWM consists of two triangular carriers as shown in Figure 11.
2. Different DC-link converters voltages (chosen as  $v_{Ca} = \frac{4}{3}v_C$  and  $v_{Cb} = \frac{2}{3}v_C$ ): In such case the PD-PWM

consists of three triangular carriers as shown in Figure 12.

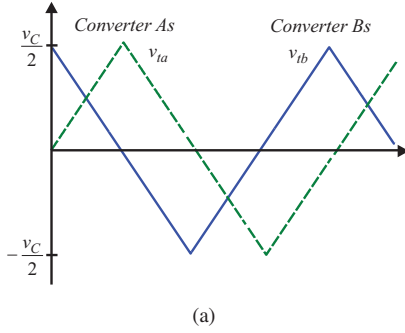


Fig. 10. Triangular carrier signals - PS-PWM technique.

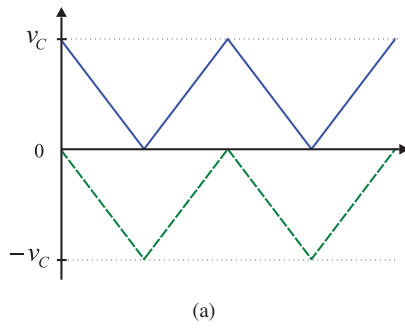


Fig. 11. Triangular carrier signals for the PD-PWM and same DC-link capacitor voltages.

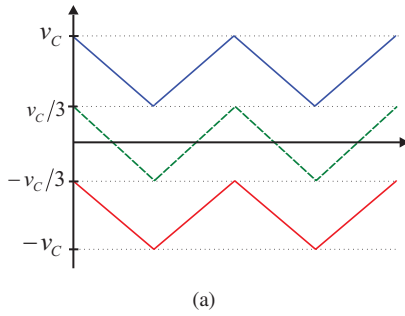


Fig. 12. Triangular carrier signals for the PD-PWM and different DC-link voltages  $v_{Ca} = \frac{4}{3}v_C$ ;  $v_{Cb} = \frac{2}{3}v_C$ .

From the equivalent circuit of the machine side converter shown in Figure 5, the converter voltages  $v_{srj} = v_{sa j 0_a} - v_{sb j 0_b}$ ,  $j = 1 \dots 5$ , is the series combination of two two-level legs with switching states  $q_{sa j}$  and  $q_{sb j}$ , respectively. By considering each switching state as a binary variable (in which  $q_{snj} = 1$  indicates a closed switch and  $q_{snj} = 0$  indicates an open one) this converter voltage has three voltage levels in the case of same DC-link voltages and four voltage levels in case of  $v_{Ca} = \frac{4}{3}v_C$  and  $v_{Cb} = \frac{2}{3}v_C$ , as shown in Figure 13 and Tables I and II. The phase voltage  $v_{sj}$ , as already mentioned, has seventeen possible voltage levels in case of same DC-link voltage and twenty five if  $v_{Ca} = \frac{4}{3}v_C$  and  $v_{Cb} = \frac{2}{3}v_C$ . In order to show the number of voltage levels

TABLE I

Vectors and voltages generated by the phase  $j$  of the proposed topology - Machine Side (same DC-link voltages).

Binary States $[q_{sa j}, q_{sb j}]$	$v_{sa j 0_a}$	$v_{sb j 0_b}$	$v_{sr j}$
[0, 0]	$-v_C/2$	$-v_C/2$	0
[0, 1]	$-v_C/2$	$v_C/2$	$-v_C$
[1, 0]	$v_C/2$	$-v_C/2$	$v_C$
[1, 1]	$v_C/2$	$v_C/2$	0

TABLE II

Vectors and voltages generated by the phase  $j$  of the proposed topology - Machine Side (different DC-link voltages).

Binary States $[q_{sa j}, q_{sb j}]$	$v_{sa j 0_a}$	$v_{sb j 0_b}$	$v_{sr j}$
[0, 0]	$-v_{Ca}/2$	$-v_{Cb}/2$	$-v_C/3$
[0, 1]	$-v_{Ca}/2$	$v_{Cb}/2$	$-v_C$
[1, 0]	$v_{Ca}/2$	$-v_{Cb}/2$	$v_C$
[1, 1]	$v_{Ca}/2$	$v_{Cb}/2$	$v_C/3$

in the machine phase voltage of the proposed configurations and the conventional ones, in Figures 8(a)-(d) are shown the machine phase voltage  $v_{s1}$  for the three-phase conventional AC drive system (Figure 1); for the five-phase conventional AC drive system (Figure 2); for the five-phase machine in open-end winding configuration with PD-PWM and same DC-link voltages; and for the five-phase machine in open-end winding configuration with PD-PWM and  $v_{Ca} = \frac{4}{3}v_C$  and  $v_{Cb} = \frac{2}{3}v_C$ . In Figures 9(a)-(c) are shown the machine phase voltage  $v_{s1}$  for the conventional five-phase AC drive system; for the five-phase machine in open-end winding configuration with same triangular carrier for both converters; and for the five-phase machine in open-end winding configuration with PS-PWM.

#### A. Harmonic Distortion

The Weighted Total Harmonic Distortion (WTHD) is used to measure the voltages harmonic content. The WTHD is defined as

$$WTHD = \frac{100}{a_1} \sqrt{\sum_{h=2}^{N_h} \left(\frac{a_h}{h}\right)^2} \quad (53)$$

where  $a_1$  is the amplitude of the fundamental component;  $a_h$  is the amplitude of  $h^{th}$  harmonic component; and  $N_h$  is the number of harmonics to be considered for the calculation of WTHD and  $h$  is the harmonic order. The phase current  $i_{sj}$  is a filtered version of the phase voltage  $v_{sj}$ . Thus, the WTHD of voltages  $v_{sj}$  is closely related to the THD of the machine currents.

In Table III is shown the WTHD of the machine phase voltage,  $v_{sj}$ , for the conventional three-phase configuration ( $C - 3ph$ ); for the conventional five-phase configuration ( $C - 5ph$ ); and for the proposed open-end winding configurations (Conf. I and II) in several different conditions of DC-link voltages and apportioning factors. The switching frequency is equal to  $10kHz$ . From Table III the smaller WTHD of the machine voltages is achieved in the open-end winding configuration with  $\mu_{0b0a}^* = 1.0$  and PD-PWM with different DC-link capacitor voltages. In such scenario the WTHD is

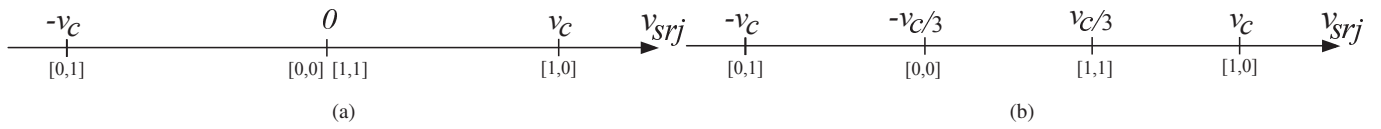


Fig. 13. Converter voltage  $v_{srlj} = v_{saj0a} - v_{sbj0b}$  at the five-phase machine side for (a) same DC-link voltages and (b) different DC-link voltages.

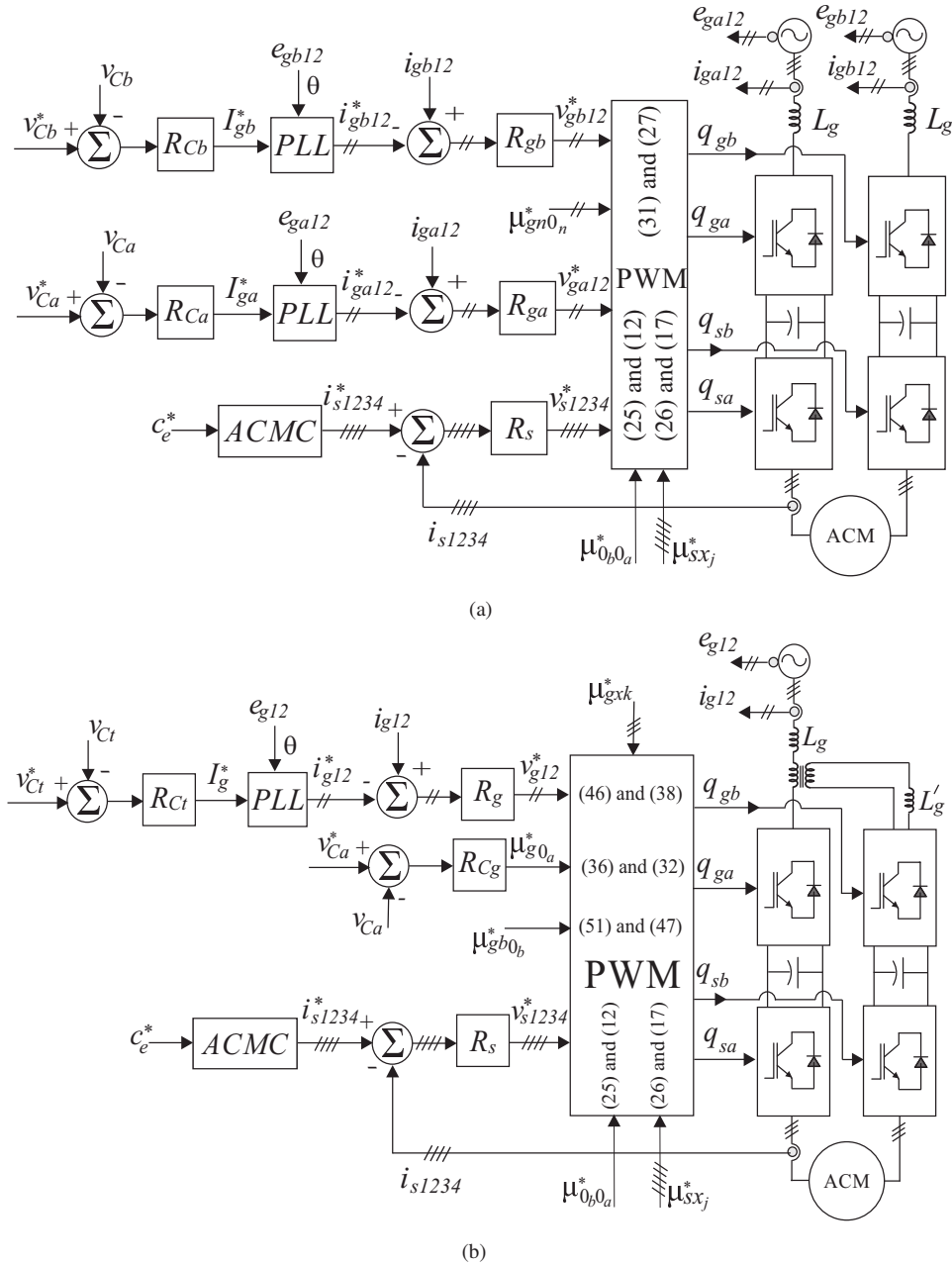


Fig. 14. Block diagram of the control system for (a) Conf. I and (b) Conf. II.

about 33% of the one obtained with the conventional five-phase configuration (Figure 2).

## V. CONTROL STRATEGY

Figure 14 presents the control block diagram of both configurations. In the case of Conf. I, Figure 14(a), the capacitor DC-link voltages  $v_{Ca}$  and  $v_{Cb}$  are adjusted to

their reference value  $v_{Ca}^*$  and  $v_{Cb}^*$  using conventional  $PI$  controllers, blocks  $R_{Ca}$  and  $R_{Cb}$ . These controllers provide the amplitude of the reference phase currents  $i_{ga12}^*$  ( $i_{ga1}^*$  and  $i_{ga2}^*$ ) and  $i_{gb12}^*$  ( $i_{gb1}^*$  and  $i_{gb2}^*$ ). To control the power factor and harmonic content at the grid side, the reference phase currents  $i_{ga12}^*$  and  $i_{gb12}^*$  are synchronized with the grid voltages  $e_{ga12}$  and  $e_{gb12}$  through a  $PLL$  (Phase Locked Loop)



**TABLE III**

**Phase voltage ( $v_{sj}$ ) harmonic distortion for the conventional three-phase and five-phase configurations and for the proposed open-end winding configurations.**

Topology	WTHD(%)
$C - 3ph$	0.1933
$C - 5ph$	0.2564
Conf. I and II ( $\mu_{0b,0a}^* = 0.5$ ) - same DC-link voltages	0.1486
Conf. I and II ( $\mu_{0b,0a}^* = 1.0$ ) - same DC-link voltages	0.1166
Conf. I and II ( $\mu_{0b,0a}^* = 0.5$ ) - different DC-link voltages	0.0868
Conf. I and II ( $\mu_{0b,0a}^* = 1.0$ ) - different DC-link voltages	0.0859

**TABLE IV**

**Parameters of the PI controllers  $R_{Ca}$ ,  $R_{Cb}$ ,  $R_{ga}$  and  $R_{gb}$  of Figure 14(a) - Conf. I.**

Controllers	Gains	
	$k_p$	$k_i$
$R_{Ca}, R_{Cb}$	1	100
$R_{ga}, R_{gb}$	25	1000

**TABLE V**

**Parameters of the PI controllers  $R_{Ct}$ ,  $R_{Cg}$  and  $R_g$  of Figure 14(b) - Conf. II.**

Controllers	Gains	
	$k_p$	$k_i$
$R_{Ct}, R_{Cg}$	0.1	10
$R_g$	25	1000

algorithm as presented in [37]. The grid currents controllers, block  $R_g$ , are double sequence synchronous controllers [38]. The current controllers define the input reference voltages  $v_{ga1}^*$  and  $v_{ga2}^*$  ( $v_{ga3}^* = -v_{ga1}^* - v_{ga2}^*$ ) and  $v_{gb1}^*$  and  $v_{gb2}^*$  ( $v_{gb3}^* = -v_{gb1}^* - v_{gb2}^*$ ) to the PWM modulator. Since the main goal of this paper is to present the power converter analysis, the AC machine control block will not be discussed in details. Instead, it is considered that the AC machine control strategy, represented by block (ACMC), provides a set of reference phase currents (such as in field oriented control)  $i_{s1234}^*$  ( $i_{s1}^*$  to  $i_{s4}^*$ ). Then, the controller  $R_s$  defines the reference voltages  $v_{s1234}^*$  ( $v_{s1}^*$  to  $v_{s4}^*$ ) to the PWM modulator. In the case of Conf. II, see Figure 14(b), the total capacitor DC-link voltages  $v_{Ct} = v_{Ca} + v_{Cb}$  is controlled by a PI controller, block  $R_{Ct}$ , that defines the amplitude of the reference phase current of the grid. Another PI controller, block  $R_{Cg}$ , regulates the individual DC-link capacitor voltages of converters  $A_g$  and  $B_g$  through  $\mu_{g0a}^*$ . The machine control in the case of Conf. II is similar to that of Conf. I. The voltages  $v_{g12}^*$  and  $v_{s1234}^*$  are processed by the PWM block (see Section IV) to define the switching states  $q_{ga}, q_{gb}, q_{sa}$  and  $q_{sb}$ . It is shown in Tables IV and V the proportional and integral gains of each controllers for both proposed configurations.

## VI. EXPERIMENTAL AND SIMULATION RESULTS

The drive system in Figure 3 and the control block diagram in Figure 14(a) were simulated on a PSIM software. In Figures 15 and 16 are shown the DC-link voltages,  $v_{Ca}$  and  $v_{Cb}$  and the grid voltage and current,  $e_{g1a}$  and  $i_{g1a}$  achieved with the simulation program for Conf. I. The simulation was

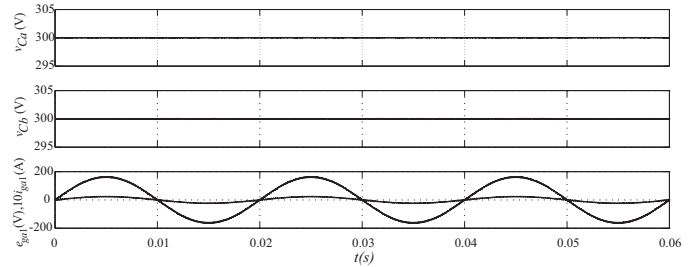


Fig. 15. Simulation results for Conf. I using same triangular carrier for all power converters.

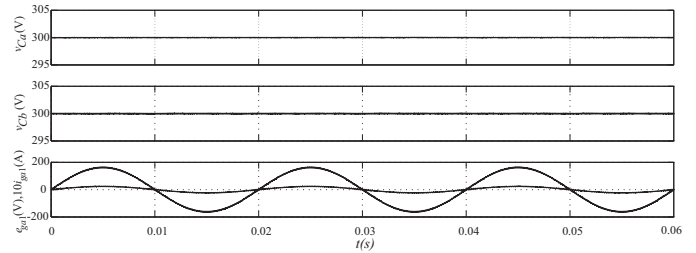


Fig. 16. Simulation results for Conf. I using two triangular carriers  $90^\circ$  apart from each other in converters  $A_s$  and  $B_s$ .

carried out using all the normalization variables of the PWM modulators equal to 0.5 (see Figure 14 for variables  $\mu_{gn0n}^*$ ,  $\mu_{0a,0b}^*$  and  $\mu_{sxj}^*$ ). Moreover, the triangular carrier signals are the same for all four converters on the results of Figure 15 and on the results of Figure 16 the machine side converters are commanded using two different triangular carriers  $90^\circ$  apart from each other. In Figure 17 are shown the simulations results for Conf. II (Figure 4) controlled by the control block diagram shown in Figure 14(b) and using PD-PWM with same DC-link voltages. It is shown in Figure 17 the DC-link

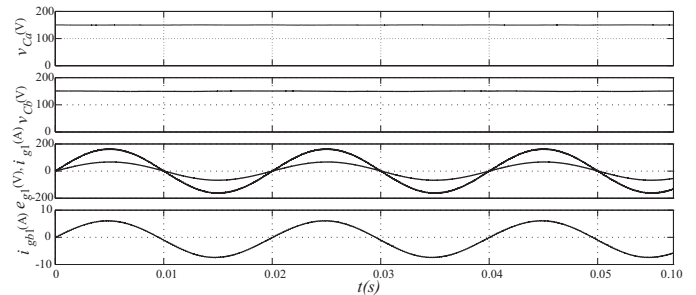
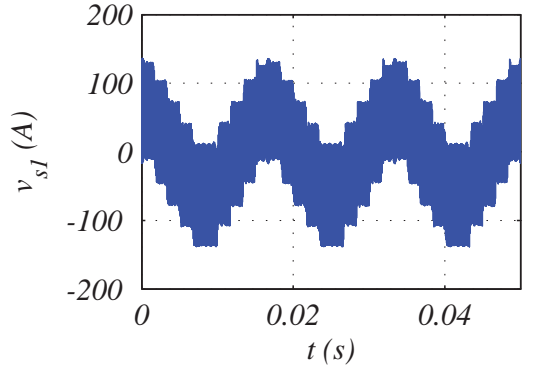
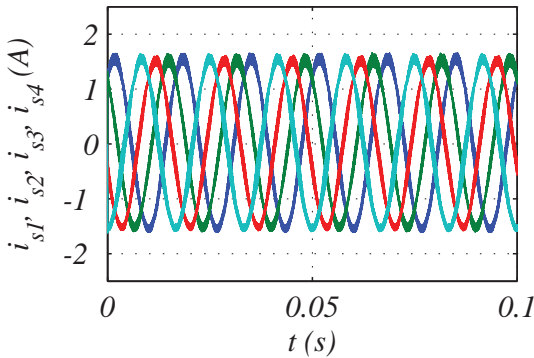


Fig. 17. Simulation results for Conf. II.



(a)



(b)

Fig. 18. Experimental results for a conventional five-phase drive system (C-5ph): (a) five-phase linear load phase voltage  $v_{s1}$ ; and (b) five-phase linear load phase currents  $i_{s1234}$ .

TABLE VI

Power ratio  $p_{A_g}/(p_{A_g} + p_{B_g})$  as a function of the variable  $\mu$  of grid side of Conf. II.

$\mu_{g_{xk}}^* \downarrow // \mu_{g_{0a}}^* \rightarrow$	$p_{A_g}/(p_{A_g} + p_{B_g})$		
	0	0.5	1
0	0.47	0.5	0.53
0.5	0.5	0.5	0.5
1	0.53	0.5	0.47
$0/1 - p_a$	0.57	0.57	0.57

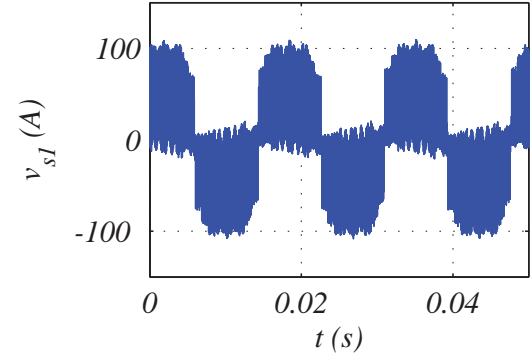
voltages,  $v_{C_a}$  and  $v_{C_b}$ , the grid voltage and current  $e_{g1}$  and  $i_{g1}$ , and the current  $i_{gb1}$  with  $\mu_{gb0_b}^* = \mu_{g_{xk}}^* = 0.5$ .

It is shown in Tables VI and VII the power ratio distribution between the power converters  $A_g$  and  $B_g$  on the grid side and between the power converters  $A_s$  and  $B_s$  on the machine side, as a function of the normalization factors. For these tables it

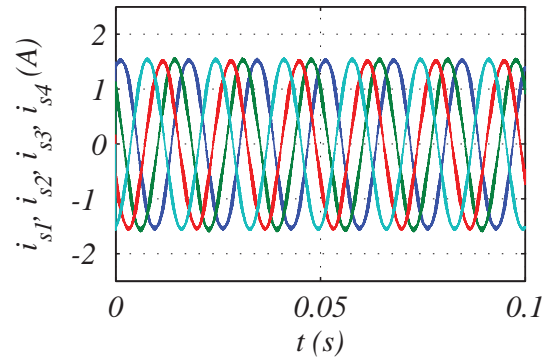
TABLE VII

Power ratio  $p_{A_s}/(p_{A_s} + p_{B_s})$  as a function of the variable  $\mu$  of the machine side.

$\mu_{s_{xk}}^* \downarrow // \mu_{s_{0a}}^* \rightarrow$	$p_{A_s}/(p_{A_s} + p_{B_s})$		
	0	0.5	1
0	0.49	0.5	0.51
0.5	0.5	0.5	0.5
1	0.51	0.5	0.49
$0/1 - p_a$	0.63	0.63	0.63



(a)



(b)

Fig. 19. Experimental results for machine side using the same triangular carrier for all converters and all normalization factors equal to 0.5: (a) five-phase linear load phase voltage  $v_{s1}$ ; and (b) five-phase linear load phase currents  $i_{s1234}$ .

TABLE VIII

System parameters used for simulation purposes and in the experimental setup.

Switching frequency	$f_{sw} = 10kHz$
Grid frequency	$f = 60Hz$
Grid voltage	$e_g = 180V_{pk}$
Grid resistance	$r_g = 0.4\Omega$
Grid inductance	$l_g = 2mH$
DC-link voltage (Conf. I)	$v_{C_a} = v_{C_b} = 300V$
DC-link voltage (Conf. II)	$v_{C_a} = v_{C_b} = 150V$
DC-link capacitance	$C = 2200\mu F$ (each)
Load resistance	$r_l = 100\Omega$
Load inductance	$l_l = 14mH$

was considered  $v_{C_a}^* = v_{C_b}^*$  and that the phase angles between  $v_{gk}$  and  $i_{gk}$  and between  $v_{sk}$  and  $i_{sk}$  are equal to  $15^\circ$ . In the case  $0/1 - p_a$  ( $\mu_{g_{xk}}^*$  adjusting the power flow through converter A), the normalization variables  $\mu_{s_{xk}}^*$  and  $\mu_{g_{xk}}^*$  are changed as a function of the current in order to increase the power of converters  $A_s$  and  $A_g$ , respectively. For other relations of the DC-link voltages  $v_{C_a}^*/v_{C_b}^*$ , the variation ranges are larger.

In Figures 18, 19 and 20 are shown some experimental results. In Figure 18 are shown the phase voltage  $v_{s1}$  and the phase currents  $i_{s1234}$  for a conventional five-phase drive system, comprised of a five-phase VSI connected to a five-phase machine. On the other hand, in Figures 19 and 20 are shown the phase voltage  $v_{s1}$  and the phase currents  $i_{s_j}$ ,

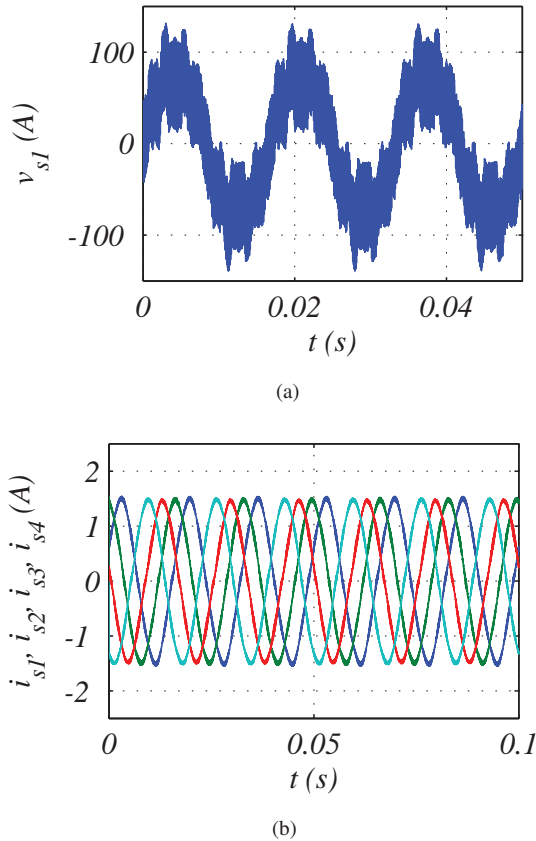


Fig. 20. Experimental results for machine side using two triangular carriers with  $90^\circ$  phase shift for converters  $A_s$  and  $B_s$  and all normalization factors equal to 0.5: (a) five-phase linear load phase voltage  $v_{s1}$ ; and (b) five-phase linear load phase currents  $i_{s1234}$ .

$j = 1, 2, 3, 4$  for Conf. I. These experimental results are representative for both configurations, since the machine side converter is the same in Conf. I and Conf. II. All experimental tests were carried out using a five-phase linear load instead of a five-phase machine. However, the main focuses of this paper is the power converter modelling and control, therefore, the results obtained with a RL load are sufficient to validate the analysis for any AC sinusoidal drive. Although the dynamic behaviour of the control system should be different if an actual machine was used. The experimental setup control system is carried out in the Texas Instruments DSP TMS320F28335.

## VII. CONCLUSIONS

This paper presented two open-end winding five-phase drive systems. The first topology, Conf. I, employs an input transformer with two secondary taps at the grid side, two three-phase three-leg converters and a ten-leg converter (totaling a sixteen legs). The second one employs a low-power series transformer at the grid side, two three-phase three-leg converters, and a ten-leg converter. The proposed configurations permit to reduce the harmonic distortion, the converter power rating, as well as the DC-link voltage rating.

Simulated and experimental results are presented.

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