AN AUTONOMOUS HARMONIC FILTERING STRATEGY FOR DISTRIBUTED ENERGY RESOURCES CONVERTERS IN MICROGRID

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Abstract - Distributed generation based on emerging energy technologies has become an attractive alternative to the conventional centralized power stations, and has drawn much interest due to the increasing demand of premium electric power. The Microgrid is a great example of integrating distributed energy resources through power electronics interface converters for grid-connected or islanding operation. This paper presents a cooperative harmonic filtering strategy for the interface converters of distributed energy sources to address harmonic issues in a low-voltage Microgrid system. A droop control method based on the reactive volt-ampere consumption of harmonics of each interface converter is designed and implemented, to accomplish the overall harmonic filtering workload can be evenly shared among converters without any communications. The operation principle is discussed in details. Computer simulations and laboratory test results are also presented to validate the distributed harmonic damping capability of the proposed strategy.

Keywords – Distributed generation systems, Microgrid, harmonic droop control, harmonic damping.

I. INTRODUCTION

The development of distributed energy resources (DERs) technologies, such as photovoltaics, wind power, fuel cells and micro turbines, have been making great strides. By integrating DERs through power electronics converters, the Microgrid [1, 2] is one of the key technologies of distributed power systems which deliver premium electric power with high quality and reliability. Based on frequency and voltage droop controls, fundamental real power and reactive power can be shared among various DER converters in a decentralized fashion without any communication systems [3–6].

As the generation capacity within the Microgrid is often limited, the harmonic current drawn by nonlinear loads could easily result in harmonic voltage distortion. The concentration of DER converters also induces harmonic resonances [7, 8]. Various control techniques for reducing output voltage distortion of the inverter have been presented, including installing passive filters and employing active damping control [9–11]. However, these methods are intended for a single converter only. Bandwidth-harmonic power droop has been proposed to share the harmonic power among multiple converters [12]. High frequency signals of small magnitude are injected by the converter and sensed back to facilitate its

active filter, in which the active filter behaves as a harmonic rters conductance, to reduce voltage harmonics in the power system [8]. An autonomous harmonic filtering strategy is presented in this paper for the DER converters in the Microgrid system [14]. In addition to the real power-frequency (P - f)droop and the reactive power-voltage (Q - V) droop controls, the DER converters operate as an active harmonic conductance to absorb harmonic current, and a droop control between the active harmonic conductance (G) and the harmonic

the active harmonic conductance (G) and the harmonic reactive power (H) is proposed to accomplish even sharing of harmonic filtering workload. The proposed G - H droop can be integrated together with the P - f droop and the Q - Vdroop of the DER converters so they can share the real power, the reactive power and the harmonic reactive power in a truly autonomous fashion without any communications.

control. This method requires high PWM frequency with fine

resolution, and thus is suitable for applications of lower kVA

rating. Blaabjerg et al. propose an inverter which operates

as an active inductor at a certain harmonic frequency to

absorb the harmonic current produced by nonlinear loads [13].

This approach is suitable if converters are installed at the

same location. Akagi et al. propose the voltage detection

II. OPERATION PRINCIPLES

A simplified one-line diagram of a low-voltage Microgrid system is shown in Figure 1. Multiple DER converter units ($DCU_x, x = 1 \cdots N$), implemented by voltage source inverters, are installed in various locations within the system. The control of each DCU consists of the droop controller and the voltage controller. The droop controller determines the fundamental voltage command and the harmonic conductance command of the inverter based on the P - f, Q - V and G - Hdroop characteristics. The fundamental voltage command and the harmonic conductance command are then passed to the voltage controller to establish the desired power output and harmonic voltage suppression characteristic. Operation principles are elaborated as follows.

A. Droop controller

The droop controller calculates the power output of each DCU, and then determines the fundamental voltage command and the harmonic conductance command. The real power, reactive power and harmonic var can be calculated as follows [15, 16],

$$\begin{bmatrix} p \\ q \end{bmatrix} = \begin{bmatrix} P + \tilde{p} \\ Q + \tilde{q} \end{bmatrix} = \begin{bmatrix} v_{\alpha} & v_{\beta} \\ -v_{\beta} & v_{\alpha} \end{bmatrix} \cdot \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix}$$
(1)

$$H = \sqrt{(\tilde{p}_{RMS})^2 + (\tilde{q}_{RMS})^2}$$
(2)

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Fig. 1. Multiple distributed generation units in an islanding network and the control block diagram of the proposed harmonic filtering strategy.

where p, q are the instantaneous real power and the instantaneous reactive power, respectively, \tilde{p}_{RMS} and \tilde{q}_{RMS} represent rms values of \tilde{p} and \tilde{q} , respectively. The DC component P and Q represent the real power and the reactive power at the fundamental frequency, and H is the harmonic reactive power.

The active harmonic conductance command G_x^* is a control gain of DCUx for suppressing voltage harmonics. DCUx appears resistive at harmonic frequencies to absorb harmonics current, and to damp harmonics resonance. G_x^* , ω_x^* , and E_x^* of the DCUx are determined by the G - H, Q - f, and P - V droop characteristics as follows,

$$G_x^* = G_0 - b_x \cdot (H_{0x} - H_x)$$

$$\omega_x^* = \omega_0 - m_x \cdot (P_{0x} - P_x)$$

$$T_x^* = E_x - (Q_x - Q_x)$$
(3)

$$E_x^* = E_0 - n_x \cdot (Q_{0x} - Q_x)$$

where

 b_x : harmonic droop coefficient; m_x : frequency droop coefficient; n_x : voltage droop coefficient; G_0 : rated conductance; ω_0 : nominal frequency; E_0 : rated phase voltage magnitude; H_{0x} : harmonic var rated capacity; Q_{0x} : reactive power rated capacity; P_{0x} : real power rated capacity.

If the P-f and the Q-V droop characteristics of all DCUs are defined as

$$m_1 \cdot P_{01} = m_2 \cdot P_{02} = \dots = m_x \cdot P_{0x} = \dots = m_N \cdot P_{0N}$$

$$n_1 \cdot Q_{01} = n_2 \cdot Q_{02} = \dots = n_x \cdot Q_{0x} = \dots = n_N \cdot Q_{0N}$$
(4)

then the real power and the reactive power can be shared in proportion to the rated capacity of each unit without any communications [3].

$$P_{1}: P_{2}: \dots : P_{x}: \dots : P_{N}$$

$$= P_{01}: P_{02}: \dots : P_{0x}: \dots : P_{0N}$$

$$Q_{1}: Q_{2}: \dots : Q_{x}: \dots : Q_{N}$$

$$= Q_{01}: Q_{02}: \dots : Q_{0x}: \dots : Q_{0N}$$
(5)

Based on the P - f droop and the Q - V droop, the fundamental output voltage command $E^*_{x_{abc}}$ can be determined.

The G - H droop is defined in a similar fashion as follows,

$$b_1 \cdot H_{01} = b_2 \cdot H_{02} = \dots = b_x \cdot H_{0x} = \dots = b_N \cdot H_{0N}$$
(6)

The harmonic var consumption of the DCU primarily results from the fundamental voltage at the installation point and its harmonic current. Since the fundamental line voltages within the network is sufficiently close, the G - H droop control allows even sharing of harmonic var among DCUs.

$$H_1: H_2: \dots : H_x: \dots : H_N = H_{01}: H_{02}: \dots : H_{0x}: \dots : H_{0N}$$
(7)

The G - H droop determines the harmonic conductance command G_x^* for voltage harmonics suppression.

With the P - f, Q - V, and G - H droop controllers, the DCUs can adjust the output fundamental frequency, the voltage magnitude and the harmonic conductance independently so the DCUs can share real power, reactive power, and harmonic var without any communications.

B. Voltage controller

The voltage controller takes orders from the harmonic conductance command G_x^* and the voltage command $E_{x_{abc}}^*$ of the droop controller, and generates PWM switching signals of the DCU inverter. The three-phase voltage $E_{x_{abc}}$ is measured and transformed into $E_{x_{qd}}^e$ in the synchronous reference frame. The fundamental voltage $\bar{E}_{x_{qd}}^e$ can be extracted by low-pass filters (LPF) from $E_{x_{qd}}^e$, and the harmonic voltage $\tilde{E}_{x_{qd}}^e$ can be obtained by subtracting $\bar{E}_{x_{qd}}^e$ from $E_{x_{qd}}^e$. The voltage harmonics $\tilde{E}_{x_{qd}}^e$ is multiplied by the harmonic conductance command G_x^* to generate harmonic current commands $\tilde{i}_{x_{qd}}^{e*}$ of the inverter.

The fundamental current command $\bar{i}_{x_{qd}}^{e*}$ is generated by the closed-loop proportional-integral (PI) control between the fundamental voltage reference $E_{x_{qd}}^{e*}$ of the droop controller and the fundamental voltage $\bar{E}_{x_{qd}}^e$ extracted by LPF from $E_{x_{qd}}^e$. The decoupling between the d^e and q^e axes components is also included. The total current command $i_{x_{qd}}^{e*}$ consists of the fundamental current command $\bar{i}_{x_{qd}}^{e*}$ and the harmonic current command $\tilde{i}_{x_{qd}}^{e*}$ to facilitate the control of both the fundamental power and harmonics suppression.

The synchronous reference frame current command $i_{x_{qd}}^{e*}$ is then transformed back to the three-phase current command $i_{x_{abc}}^*$. Based on $i_{x_{abc}}^*$, the measured current $i_{x_{abc}}$, and the measured voltage $E_{x_{abc}}$, the current regulator calculates the voltage command $v_{x_{abc}}^*$ as,

$$v_{x_{abc}}^{*} = \frac{L_{x}}{\Delta T} (i_{x_{abc}}^{*} - i_{x_{abc}}) + E_{x_{abc}}$$
(8)

where L_x is the output inductor of the inverter, and ΔT is the sampling period of the digital controller. In order to track the current command with a high bandwidth, the spacevector PWM is employed to generate the corresponding gating signals so the inverter can synthesize the desired current.



Fig. 2. Simulation circuit.

TABLE IDCU parameters.

	m(rad/s/W)	n(1/A)	$b(1/V^2)$	$P_0(kW)$	$Q_0(var)$	$H_0(kvar)$	$G_0(1/\Omega)$
DCU ₁	-10^{-5}	-10^{-3}	-10^{-2}	5.0	0	2.0	0
DCU_2	-10^{-5}	-10^{-3}	-10^{-2}	5.0	0	2.0	0

III. SIMULATION RESULTS

The proposed harmonic filtering method is applied to demonstrate the damping performances and the effectiveness of the G - H droop control. Figure 2 is a simulation circuit of

A. $t < 1.0 \, \text{s}$

Initially, both DCU_1 and DCU_2 supply linear loads without any droop controls. Figure 3 shows the power consumption of each DCU is quit unequally distributed.

B.
$$1.0 \,\mathrm{s} < t < 1.5 \,\mathrm{s}$$

After t = 1.0 s, the real power and the reactive power are evenly shared due to the Q - f droop and P - V droop.

C.
$$1.5 \,\mathrm{s} < t < 2.0 \,\mathrm{s}$$

At t = 1.5 s, all nonlinear loads are switched in, but the harmonic filtering functionality of the DCUs is not yet employed, ie. $G_1^* = G_2^* = 0$. The sharing of real power and reactive power remains, and the harmonic current of both DCUs results in increased harmonic var as indicated by H_1 and H_2 . Figure 4(a) shows the line voltages are significantly distorted due to the lack of harmonic filtering. The voltage THDs of bus A, B, and C reach 9.2%, 9.5%, 9.0% respectively.

D.
$$2 \,\mathrm{s} < t < 2.5 \,\mathrm{s}$$

The G - H droop controls of both DCUs are enabled at t = 2 s. Figure 4(b) shows that the voltage THDs of bus A, B, and C are 1.9%, 2.3%, 1.5% respectively, all significantly reduced compared to the results in Figure 4(a). At the steady state, DCU₁ absorbs $H_1 = 1892$ var with $G_1^* = 2.17 \Omega^{-1}$ and DCU₂ absorbs $H_2 = 1864$ var with $G_2^* = 2.72 \Omega^{-1}$. The dominant harmonic current components of DCU₁ and DCU₂ are $i_1^{5th} = 3.85$ A, $i_1^{7th} = 2.80$ A, $i_2^{5th} = 3.80$ A, $i_2^{7th} = 2.75$ A, as illustrated in Figure 4(e). The harmonic filtering workload is evenly shared between two DCUs thanks to the G - H droop control.

Figure 4(c) shows the waveforms if both DCU₁ and DCU₂ operate with fixed conductance command, $G_1^* = G_2^* = 2.5 \,\Omega^{-1}$. At the steady state, DCU₁ consumes 2040 var and DCU₂ consumes 1760 var. Figure 4(f) shows $i_1^{5th} = 4.09 \,\text{A}$, $i_1^{7th} = 3.19 \,\text{A}$, $i_2^{5th} = 3.59 \,\text{A}$, $i_2^{7th} = 2.67 \,\text{A}$. Compared to the G - H droop control, the fixed conductance operation results in uneven sharing of harmonic filtering workload, and may cause overloading of certain DCUs.

IV. LABORATORY TEST RESULTS

Figure 5 shows the laboratory test bench. DCU_1 and DCU_2 are deployed at bus A and bus B, respectively. The system parameters are given as follows,

- Power system: 110 V (line-to-line), 60 Hz.
- DCUs: Conventional voltage source inverters with PWM frequency of 20 kHz. The droop parameters are as follows, $G_0 = 0 \Omega^{-1}$,



Fig. 3. Distributions of the real power, the reactive power, and the harmonic var. (solid line:DCU₁; dash line:DCU₂)



Fig. 4. The voltages, currents, fifth harmonic currents, and seventh harmonic currents of both DCUs in different operation modes.



Fig. 5. Laboratory test bench.

$$\begin{split} m_1 &= m_2 = -1 \times 10^{-5} \, \mathrm{rad/s} \cdot \mathrm{W}^{-1}, \\ n_1 &= n_2 = -1 \times 10^{-3} \, \mathrm{A}^{-1}, \\ b_1 &= b_2 = -1 \times 10^{-2} \, \mathrm{V}^{-2}, \\ P_{01} &= P_{02} = 1 \, \mathrm{kW}, \\ Q_{01} &= Q_{02} = 0 \, \mathrm{kvar}, \\ H_{01} &= H_{02} = 100 \, \mathrm{var}. \end{split}$$

Figure 6 shows harmonic var and harmonic conductance commands of both DCUs. When $t < T_0$, both DCUs are off. At $t = T_0$, DCU₁ is started (both switch S_1 and switch S_5 close) and then nonlinear load is turned-on (switch S_3 closes). DCU₁ supplies all the fundamental power and the harmonic filtering var, whereas DCU₂ runs under the phase lock mode with zero current command until $t = T_1$. At this time interval, H_2 is due to the distorted line voltage at BUS B and the current ripple. After $t = T_1$, the droop control of DCU₂ is engaged, and thus DCU₂ gradually increases its power and harmonic var output. At the same time, G_1 reduces slightly because of the G - H droop control as shown in Figure 6. At the steady state, both DCUs evenly share the real power and harmonic filtering var. The steady-state sharing of harmonic var is given in Figure II(a). When $t = T_2$, a newly added linear load (switch S_4 closes) causes slight decreasing of harmonic distortion. Therefore, the conductance commands of both DCUs are increased to maintain sharing of harmonic var between both DCUs, as given in Figure II(b).

TABLE II The harmonic conductance command, the harmonic var, the voltage THD, and the real power of both DCUs in Figure 6.

	0			
(a)	During T_1	< t	<	T_2 .

	$G(\Omega^{-1})$	H(var)	VTHD(%)	P(W)
DCU_1	0.17	84	3.5	200
DCU ₂	0.19	81	3.1	200

(b) During $t > T_2$.

	$G(\Omega^{-1})$	H(var)	VTHD(%)	P(W)
DCU_1	0.30	70	2.7	300
DCU ₂	0.34	66	2.4	300

V. DISCUSSION

The G-H droop control manipulates the harmonic conductance of each DCU to achieve the proportional sharing of the total harmonic reactive power of the load.



Fig. 6. Time response of the harmonic var, the harmonic conductance command, and the real power for both DCUs with the same rated capacity, H_1, H_2 :^{100 var/div}, G_1, G_2 :^{0.1 Ω^{-1}/V}, X axis: ¹⁰%div.

However, the power line impedance could also affect the flow of harmonic current. Also, in the low voltage Microgrid, the line tends to have higher resistive content than the conventional transmission/distribution network as previous literatures have pointed out [17, 18]. The performance of the G-H droop control is examined under these circumstances using a simplified circuit as shown in Figure 7.



Fig. 7. Simplified one-line diagram of the harmonic producing load and the DCUs' harmonic conductances.

The harmonic current source I_h represents the harmonic current of a 1.0 pu. nonlinear load with 0.2 pu., 0.15 pu., 0.9 pu. and 0.77 pu. of the 5th, 7th, 11th and 13th harmonic current respectively.

The harmonic current and the harmonic reactive power

absorbed by each DCUs can be represented as

$$I_1 = \frac{\frac{1}{G_2} + Z_{t2}}{\frac{1}{G_1} + \frac{1}{G_2} + Z_{t1} + Z_{t2}}$$
(9)

$$I_2 = \frac{\frac{1}{G_1} + Z_{t1}}{\frac{1}{G_1} + \frac{1}{G_2} + Z_{t1} + Z_{t2}}$$
(10)

$$H_1 = E_{rms} \cdot G_1 \cdot I_{1,rms} \tag{11}$$

$$H_2 = E_{rms} \cdot G_2 \cdot I_{2,rms} \tag{12}$$

The line impedance Z_2 is assumed to be 0.075Ω , $0.075 \angle (\frac{\pi}{4}) \Omega$, and $0.075 \angle (\frac{\pi}{2}) \Omega$, and Z_1 varies from 0 to 0.15Ω at the same impedance angle of Z_2 . In order to verify if the G-H droop control can accomplish even sharing of the harmonic reactive power, the ratio of $\frac{H_1}{H_2}$ and their G_1 and G_2 commands are plotted in Figure 8 and Figure 9 for the droop slope of $-2 \times 10^{-2} \,\mathrm{V}^{-1}$ and $-5 \times 10^{-3} \,\mathrm{V}^{-1}$ respectively. The G-H droop settings of both DCUs are identical, thus the harmonic VARs should split evenly between them.

Figure 8 shows that the harmonic reactive power sharing of G-H droop is affected by the varying line impedance Z_1 . For the mismatch of -30% and +30% of the line impedances Z_1 and Z_2 , the ratio H_1/H_2 deviates in the range of +47% \sim -24% in the case of inductive line, and $+15\%~\sim~-12\%$ in the case of resistive line. The G-H droop is more effective in the case of resistive line because the active conductance commands G_1 and G_2 of both DCUs are also resistive, they have direct impact on the current division as given in Figure 12. For the inductive line, the active conductance commands affect the current division through a quadratic relationship with the reactance, and the G-H droop is not as effective in terms of the sharing of harmonic VARs. Also, for higher order harmonics, the line impedance grows proportionally with the harmonic frequency, while the resistive line impedance remains the same across the spectrum. Thus the conductance commands become less effective for the high order harmonics. This can be improved if separate conductance commands are adopted for different harmonic frequencies [19]. The comparison between Figure 8 and Figure 9 also shows that the steeper droop slope results in more balanced sharing when the line impedance $|Z_1|$ is small. As $|Z_1|$ increases, the line impedance dominates the current division, and the active conductance commands become less effective in balancing the harmonic VARs.

VI. SUMMARY

An autonomous harmonic filtering strategy is proposed for distributed energy resource converters in the Microgrid. The harmonic conductance-harmonic var (G - H) droop control is developed to accomplish balanced distribution of harmonic filtering workload among multiple DCU converters. With proper settings of the P - f, Q - V, and G - H droop controls as given in Figure 3, Figure 4, Figure 5 and Figure 7, each unit can share the real power, the reactive power and the harmonic filtering workload based on its own rated capacity without any communications. The P - f and Q - Vdroop methods have been widely accepted for the distributed controls of power converters. The proposed G - H droop



(a) Sharing of harmonic reactive power H_1 and H_2 .



(b) Harmonic conductance commands G_1 and G_2 .

Fig. 8. Effect of line impedances on the G-H droop; droop slope $b = -2.0 \times 10^{-2} V^{-3}.$



(a) Sharing of harmonic reactive power H_1 and H_2 .



(b) Harmonic conductance commands G_1 and G_2 .

Fig. 9. Effect of line impedances on the G-H droop; droop slope $b = -5.0 \times 10^{-3} V^{-1}$.

control can be seamlessly integrated with P - f and Q - Vdroop controls to provide harmonic voltage damping within an islanding network. The G - H droop control can also reduce the harmonic voltage distortion in the grid-connected operation [20, 21]. The impact of the line impedance on the G - H droop control is also investigated. The G - Hdroop characteristics need to be tuned to ensure that the active harmonic conductance commands of DCUs are sufficiently significant compared to the line impedance. This could be done by vertically shifting the droop lines or adjusting the rated capacities of DCUs [3, 22]. In general, the G - H droop control is more effective if the line is resistive as shown in the previous analysis. Thus it is suitable for the low-voltage Microgrid applications.

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