# **A MMRAC CONTROLLER APPLIED TO ENCODERLESS SPEED CONTROL INDUCTION MOTOR DRIVES**

H.T. Câmara, H. A. Gründling UFSM/CT/GEPOC Federal University of Santa Maria. Santa Maria, Av. Roraima s/n, Brazil email: htcamara@hotmail.com

*Abstract –***This paper proposes a Modified Model Reference Adaptive Controller (MMRAC) for a speed sensorless induction motor drive. MMRAC is obtained by modifying the control law** *U* **of a Robust Model Reference Adaptive Controller (RMRAC). The MMRAC is used to assure performance in a wide speed range, including lowand zero-speed conditions. Experimental results are given to show the effectiveness of the proposed controller.** 

*Keywords –* **Speed Sensorless, Induction Motor Drive, Recursive Least Square, RMRAC.** 

## NOMENCLATURE



## I. INTRODUCTION

For a decade, induction motor (IM) drive-based electrical actuators have been under investigation as potential replacement for conventional hydraulic and pneumatic actuators in aircraft. Advantages of electric actuator include lower weight and size, reduced maintenance and operating costs, improved safety due to the elimination of hazardous fluids and high pressure hydraulic and pneumatic actuators, and increased efficiency.

Recently, research efforts have been devoted to eliminate speed sensor coupled to the shaft of the motor, presented in conventional closed loop servo systems. Motivations for substitution of speed sensor in estimation techniques are cost (usually a speed sensor is an expensive component) and reliability (this sensor is delicate and its signal can be interfered by electromagnetic sources).

In recent years, several encoderless vector control schemes have been proposed: algorithms using Kalman-filter [3]-[4], model reference adaptive systems [5]-[6], direct control of torque and flux [7]-[8], and linear models [12]-[1]. In Reyes et al [12] and Minami et al [1] a recursive algorithm is proposed to estimate the rotor speed based on measurements of stator voltages and currents. This technique is designed by two linear regression models derived from the machine electrical equations. However, all these techniques are based on back EMF measurement, and fail at low and zero speed because induced voltage levels are too low to be correctly measured. Moreover no voltages are induced on the stator windings at zero frequency.

Sensorless techniques based on estimation airgap flux position by using the third harmonic component of the stator voltage have been developed to improve the performance of EMF based DFOC drives [13]-[14]. These methods are based on the detection of the ripple generate on the angular frequency of the rotor flux by the injection of a suitable high frequency stator current signal. The rotor speed is estimated as a function of the rotor flux angular frequency ripple, the injected signal and the stator currents. Consequently these methods are motor parameters independent and allow estimating rotor speed at low and zero stator frequency, but these techniques can produce torque ripple and saturation in the main path and around the rotor slots, generating an additional modulation which interferes in the rotor speed estimation.

 $\overline{a}$ 

Manuscript received February 4, 2005; first revised April 4, 2005; second review July 4, 2005. Recommended by Editor José Antenor Pomilio.

$$
\begin{bmatrix}\n\mathbf{i} \\
I_{ds} \\
I_{qs} \\
\mathbf{j} \\
\mathbf{k} \\
\mathbf{k} \\
\mathbf{k} \\
\mathbf{r}_{qr}\n\end{bmatrix} = \begin{bmatrix}\n-\frac{R_{S}}{\overline{\sigma}L_{S}} & \omega + \frac{n_{p}\omega_{R}L_{M}^{2}}{\overline{\sigma}L_{S}L_{R}} & \frac{R_{R}.L_{M}}{\overline{\sigma}L_{S}L_{R}} & \frac{n_{p}\omega_{R}L_{M}}{\overline{\sigma}L_{S}} \\
-\omega - \frac{n_{p}\omega_{R}L_{M}^{2}}{\overline{\sigma}L_{S}L_{R}} & -\frac{R_{S}}{\overline{\sigma}L_{S}} & -\frac{n_{p}\omega_{R}L_{M}}{\overline{\sigma}L_{S}} & \frac{R_{R}L_{M}}{\overline{\sigma}L_{S}L_{R}} \\
\mathbf{i} \\
\mathbf{j}_{qr} \\
\mathbf{k} \\
\mathbf{k} \\
\mathbf{r}_{qr}\n\end{bmatrix} = \begin{bmatrix}\n-\frac{R_{S}}{\overline{\sigma}L_{S}} & \omega + \frac{n_{p}\omega_{R}L_{M}^{2}}{\overline{\sigma}L_{S}L_{R}} & \frac{R_{S}}{\overline{\sigma}L_{S}} & \frac{n_{p}\omega_{R}L_{M}^{2}}{\overline{\sigma}L_{S}} \\
\frac{R_{S}L_{M}}{\overline{\sigma}L_{S}} & -\frac{n_{p}\omega_{R}L_{M}^{2}}{\overline{\sigma}L_{S}} & -\frac{R_{R}}{\overline{\sigma}} & \omega - \frac{R_{R}}{\overline{\sigma}} \\
\frac{n_{p}\omega_{R}L_{M}^{2}}{\overline{\sigma}L_{R}} & \frac{R_{S}L_{M}^{2}}{\overline{\sigma}L_{S}L_{R}} & -\omega + \frac{n_{p}\omega_{R}^{2}}{\overline{\sigma}} & -\frac{R_{R}}{\overline{\sigma}L_{R}}\n\end{bmatrix}
$$

$$
T_E = n_P L_M \left( I_{dr} I_{qs} - I_{ds} I_{qr} \right) \tag{2}
$$

$$
J\frac{d}{dt}\omega_R + B\omega_R = T_E - T_L \tag{3}
$$

$$
\begin{bmatrix} \vec{I}_{ds} \\ \vec{I}_{gs} \end{bmatrix} = \begin{bmatrix} -\frac{R_s}{\overline{\sigma} L_s} & \omega \\ -\omega & -\frac{R_s}{\overline{\sigma} L_s} \end{bmatrix} \begin{bmatrix} I_{ds} \\ I_{gs} \end{bmatrix} + \begin{bmatrix} \frac{1}{\overline{\sigma} L_s} & 0 \\ 0 & \frac{1}{\overline{\sigma} L_s} \end{bmatrix} \begin{bmatrix} V_{ds} \\ V_{gs} \end{bmatrix}
$$
(4)  

$$
T_E = \frac{n_P L_m^2 I_{gs} I_{ds}^*}{L_R}
$$
(5)

To assure performance in a wide speed range, including low and zero speed conditions, this paper proposes the use of an estimator associated with the RMRAC control law in a speed sensorless IM servo system. A modification is proposed in the RMRAC technique to obtain the Modified Model Reference Adaptive Controller (MMRAC). The resultant controller is capable of ensuring good performance in a wide speed range, including low and zero speed conditions. Experimental results are presented to demonstrate the dynamic performance of the proposed closed-loop system.

#### II. PLANT DESCRIPTION

The *dq* model of the three-phase IM, with electrical variables referred to an arbitrary *dq* rotating frame, can be described by (1), (2) and (3), where the motor is considered perfectly balanced and regardless the saturation phenomena.  $\overline{\sigma} = 1 - L_{M}^{2}/(L_{S} L_{R})$ ,  $V_{ds}$ ,  $V_{gs}$  are the stator voltages;  $R_{S}$ ,  $R_{R}$ are the stator and rotor resistance.  $L_{S}$ ,  $L_{R}$ ,  $L_{M}$  are the stator, rotor and mutual inductances;  $I_{ds}$ ,  $I_{qs}$ ,  $I_{dr}$ ,  $I_{qr}$  are the stator and rotor currents;  $\omega$ ,  $\omega$ <sub>R</sub> are the rotating speed of the electrical current and of the shaft;  $T_E$ ,  $T_L$  are the electrical torque and the load torque; *J*, *B* are the moment of inertia and the damping coefficient (motor and load);  $n_p$  is the number of pole pairs of the motor.

Equation (2) represents the coupling between the electrical and mechanical parts, and the mechanical part is given by the equation (3).

Appling IFOC techniques in (1) and (2) results in equations (4) and (5), where (\*) define a reference signal, [11]. The  $I_{ds}$  current is kept constant to ensure a constant level of machine magnetization. This assumption is necessary to obtain linearization in (5). The frequency of the voltage applied to the IM is the rotor flux frequency given by

$$
\frac{n_{P}\omega_{R}L_{M}}{\overline{\sigma}L_{S}L_{R}}\begin{bmatrix}\nI_{ds} \\
I_{qs} \\
I_{qr}\n\end{bmatrix} + \begin{bmatrix}\n\frac{1}{\overline{\sigma}L_{S}} & 0 \\
0 & \frac{1}{\overline{\sigma}L_{S}} \\
0\n\end{bmatrix}\begin{bmatrix}\nV_{ds} \\
V_{qs} \\
V_{qs}\n\end{bmatrix}
$$
\n(1)\n
$$
-\frac{R_{R}}{\overline{\sigma}L_{R}}\begin{bmatrix}\nI_{dr} \\
I_{qr}\n\end{bmatrix} + \begin{bmatrix}\nL_{M} & 0 \\
-\frac{L_{M}}{\overline{\sigma}L_{S}L_{R}} & 0 \\
0 & -\frac{L_{M}}{\overline{\sigma}L_{S}L_{R}}\n\end{bmatrix}
$$
\n(1)\n
$$
-\frac{R_{R}}{\overline{\sigma}L_{R}}\begin{bmatrix}\nV_{ds} \\
V_{qs}\n\end{bmatrix}
$$
\n(2)

Note that the rotor speed is required to obtain the synchronous speed and to convert the measurements of the stator voltages and currents to *dq* reference frame. Here it is assumed that speed sensor can not be used. Therefore an estimation algorithm is presented in the next section to obtain  $\omega$ <sub>n</sub>.

## III. SPEED ESTIMATION ALGORITHM

Consider the three phase induction motor defined in (1)- (3) referred to the stator fixed frame.

$$
\begin{bmatrix}\nV_{ds}^{s} \\
V_{gs}^{s} \\
0 \\
0\n\end{bmatrix} = \begin{bmatrix}\na_1 & 0 & p.L_M & 0 \\
0 & a_1 & 0 & p.L_M \\
p.L_M & \omega_R L_M & a_2 & \omega_R L_M \\
0 & -\omega_R L_M & pL_M & -\omega_R L_M & a_2\n\end{bmatrix} \begin{bmatrix}\nI_{ds}^{s} \\
I_{qs}^{s} \\
I_{dr}^{s} \\
I_{dr}^{s}\n\end{bmatrix}
$$
\n(7)

where (<sup>s</sup>) defines stationary referential variables,  $a_1 = R_s + pL_s$ ,  $a_2 = R_R + pL_R$  and  $p = d/dt$ . Using equation (7), it is possible to reformulate the problem of estimating speed as a problem of estimating the parameters based on a linear regression model. Linear regression models are models that have the structure given by

$$
Y = C \hat{\omega}_R \tag{8}
$$

Considering the rotor speed as the only unknown parameter, from (7), the linear model is given by

$$
Y = \begin{bmatrix} \overrightarrow{I}_{ds}^{s} + P_1 \overrightarrow{I}_{ds}^{s} + a_3 I_{ds}^{s} - \frac{1}{\overline{\sigma} L_S} \overrightarrow{V}_{ds}^{s} - \frac{R_R}{L_S L_R \overline{\sigma}} V_{ds}^{s} \\ \overrightarrow{I}_{qs}^{s} + P_1 \overrightarrow{I}_{qs}^{s} + a_3 I_{qs}^{s} - \frac{1}{\overline{\sigma} L_S} \overrightarrow{V}_{qs}^{s} - \frac{R_R}{L_S L_R \overline{\sigma}} V_{qs}^{s} \end{bmatrix}
$$
\n
$$
C^{T} = \begin{bmatrix} -\overrightarrow{I}_{qs}^{s} - \frac{R_S}{L_S \overline{\sigma}} I_{qs}^{s} + \frac{1}{L_S \overline{\sigma}} V_{qs}^{s} \\ \overrightarrow{I}_{ds}^{s} + \frac{R_S}{L_S \overline{\sigma}} I_{ds}^{s} - \frac{1}{L_S \overline{\sigma}} V_{ds}^{s} \end{bmatrix}
$$
\n(9)

$$
\frac{V_{fds}^{s}}{V_{ds}^{s}} = \frac{V_{fgs}^{s}}{V_{gs}^{s}} = \frac{I_{fds}^{s}}{I_{ds}^{s}} = \frac{I_{fgs}^{s}}{I_{gs}^{s}} = G_{f}(s) = \frac{\omega_{c}^{3}}{(s + \omega_{c})^{3}}
$$
(10)

where  $P_1 = (R_s L_R + R_R L_s)/(L_s L_R \overline{\sigma})$ ,  $a_3 = \frac{R_s R_R}{L_s L_R}$ *S R*  $a_3 = \frac{R_s R_R}{L_s L_R \overline{\sigma}}$  and  $\omega_c = 5\omega$ , [12].



Fig. 1. Controller Structure

The regression model presented and other variations of it can be obtained from (7) with the electrical variables referred to the stator fixed frame as presented in [12]. It is assume that the derivatives presented in (9) are measurable quantities. In the implementation these quantities are obtained by state variable filters (SVF) [16]. These filters are developed by discretization of transfer function given by (10) where the inputs  $V_{ds}^{s}$ ,  $V_{qs}^{s}$ ,  $I_{ds}^{s}$  and  $I_{qs}^{s}$  are used to obtain the filtered signals  $V_{fds}^{s}$ ,  $V_{fqs}^{s}$ ,  $I_{fds}^{s}$  and  $I_{fqs}^{s}$ .

To estimate  $\hat{\omega}_R$  a recursive least squares algorithm can be

used, [2]. The recursive equations are presented as follows  
\n
$$
\widehat{\omega}_R(t) = \widehat{\omega}_R(t-1) + K(t)e(t)
$$
\n(11)

$$
e(t) = Y(t) - C^{T}(t)\hat{\omega}_{R}(t-1)
$$
\n(12)

$$
K(t) = \frac{P_R(t-1)C(t)}{1 + C^{T}(t)P_R(t-1)C(t)}
$$
(13)

$$
P_R(t) = 1 + K(t)C^{T}(t)P_R(t-1)
$$
\n(14)

By using this algorithm, it is possible to obtain the By using this argorium, it is possible to botain the estimated speed  $\hat{\omega}_R$  used in the control law presented in the next section.

## IV. CONTROLLER STRUCTURE

The proposed sensorless speed control structure is shown in Figure 1. It uses current signals measured on the stator of the machine. A MMRAC control law presented in the next section is used to obtain the  $\int_{q_s}^{*}$  current calculated by the difference between the estimated speed  $\hat{\omega}_R$  and the output of the reference model  $\omega_{RM}$ . A RMRAC controller is employed to compensate parametric variations on the mechanical plant. Moreover, the use of a speed observer to obtain a signal to be controlled by the RMRAC controller results in a sensorless controller tolerant to unmodeled dynamics.

## V. MMRAC CONTROLLER STRUCTURE

For a SISO plant (Single-Input Single-Output), a RMRAC controller can be designed as:-

$$
\omega_R = G(s)U\tag{15}
$$

$$
G(s) = G_0(s) \left[ 1 + \mu \Delta_m(s) \right] + \mu \Delta_a(s) \tag{16}
$$

where  $G(s)$  is the plant transfer function,  $G_0(s)$  is the modeled part of the plant and  $\mu\Delta_m(s)$  and  $\mu\Delta_a(s)$  are additive and multiplicative perturbations, respectively. The modeled part of the plant  $G_0(s)$  is a strictly proper transfer function, expressed as  $G_0(s) = k_p Z_0(s) / R_0(s)$ , where  $Z_0(s)$  and  $R_0(s)$ are monic polynomials of degree m and n respectively. In addition, the following assumptions on  $G_0(s)$  are made:

- S1)  $R_0(s)$  is a monic polynomial of degree n and  $Z_0(s)$  is monic Hurwitz polynomial of degree m≤(n-1);
- S2) The signal of  $\bar{k}_P$  and the values of *m* and *n* are known.

Furthermore, for the unmodeled plant part is assumed that

- S3)  $\Delta_a(s)$  is a strictly proper stable transfer function and  $\Delta_{\rm m}(s)$  is a stable transfer function;
- S4) A bound  $p_0>0$  on the stability margin p $>0$  for which the poles of  $\Delta_a(s-p)$  and  $\Delta_m(s-p)$  are stable is known.

The adaptive control objective can be described as follows. Given the reference model

$$
G_{\rm M}(s) = k_{\rm m} Z_{\rm m}(s) / R_{\rm m}(s), \ \omega_{\rm RM} = G_{\rm M}(s) \, Ref \tag{17}
$$

where  $R_m(s)$  is a Hurwitz polynomial of degree  $n^* = n - m$ , where the *Ref* is a uniformly bounded reference, design an adaptive controller so that for some  $\mu^* > 0$  and any  $\mu \in [0, \mu^*),$ the resulting closed-loop plant is stable and the plant output  $\hat{\omega}_R$  tracks the reference model output  $\omega_{RM}$  as closely as possible, despite disturbances  $\Delta_a(s)$  e  $\Delta_m(s)$ , satisfying S3 and S4.

As verified in [12], the speed estimator used has problems at very low speed. To overcome this problem, in this paper it is proposed the addition of a sigma modification function in the RMRAC controller:

$$
\hat{\omega}_{\rm Rf} = \sigma_{\rm R} \hat{\omega}_{\rm R} + (1 - \sigma_{\rm R}) \omega_{\rm RM} \tag{18}
$$

where

$$
\sigma_{R} = \begin{cases}\n0 & \text{if } \|\omega_{\text{RM}}\| < M_{R0} \\
\sigma_{R0} \left( \frac{\|\omega_{\text{RM}}\|}{M_{R0}} - 1 \right) & \text{if } M_{R0} \le \|\omega_{\text{RM}}\| < 2M_{R0} \\
\sigma_{R0} & \text{if } \|\omega_{\text{RM}}\| \ge 2M_{R0}\n\end{cases}
$$
\n(19)

The sigma modification defines when it is possible to use the signal in the control law. When  $\omega_{RM}$  is smaller than  $M_{R0}$ , the signal used in the control law feedback is  $\omega_{\text{RM}}$ . On the other hand, when  $\omega_{RM}$  is bigger than  $M_{R0}$ , the  $\hat{\omega}_R$  signal is gradually employed in the control law feedback. When  $\omega_{RM}$  is bigger than 2  $M_{R0}$ , the  $\hat{\omega}_R$  signal is appropriated to be used in the control law (22).

The input control law *U* and output  $\hat{\omega}_{Rf}$  are used to generate n-1 dimensional auxiliary vectors so that

$$
\dot{w}_1 = F w_1 + qU \tag{20}
$$

$$
\mathbf{w}_2 = F w_2 + q \,\hat{\omega}_{\text{Rf}} \tag{21}
$$

where  $F$  is a stable matrix and the  $(F,q)$  is a controllable pair. The MMRAC signal *U* is given by

$$
U = w_1 \theta_1^T + w_2 \theta_2^T + \hat{\omega}_{\text{Rf}} \theta_3 + \text{Ref}/\theta_4 \tag{22}
$$

where  $\theta_1^T$ ,  $\theta_2^T$ ,  $\theta_3$  and  $\theta_4$  are control parameters. These parameters are obtained by a modified RLS presented in [10] and described as follows.

## VI. MMRAC PARAMETER ESTIMATION ALGORITHM

In the proposed controller, a modified recursive leastsquares (RLS) algorithm is used. This basic MMRAC algorithm structure is showed in Figure 2.



Fig. 2. Robust model reference adaptive control structure

The control law parameters are obtained by

$$
\dot{\theta} = -\sigma P \theta - \frac{\varepsilon_1 P \zeta}{\bar{m}} \tag{23}
$$

where  $\boldsymbol{\theta} = [\theta_1 \theta_2 \theta_3 \theta_4]^T$ ,

$$
\dot{\boldsymbol{P}} = \lambda \overline{\mu}^2 \boldsymbol{P} - \left( \frac{\boldsymbol{P} \zeta \zeta^{\mathrm{T}} \boldsymbol{P}}{\overline{m}} + \overline{\mu}^2 \frac{\boldsymbol{P}^2}{R^2} \right)
$$
(24)

and  $P = P<sup>T</sup>$  is so that

is so that  
\n
$$
0 < P(0) \le \lambda R^2 I, \ \mu^2 \le k_\mu \overline{\mu}^2
$$
\n(25)

$$
\overline{m} = 1 + \alpha_1 \left[ m \right]^2, \quad \zeta = G_m I w \tag{26}
$$

$$
\dot{m} = \delta_0 m + \delta_1 \left( |U| + |\hat{\omega}_{Rf}| + 1 \right), \ m(0) > \frac{\delta_1}{\delta_0}, \ \delta_1 \ge 1 \tag{27}
$$

where  $\alpha_1$ ,  $\delta_0$ ,  $\delta_1$ ,  $\lambda$ ,  $\overline{\mu}$  and  $R^2$  are positive constants and  $\delta_0$ satisfies  $\delta_0 + \delta_2 \le \min[p_0, q_0]$ .  $q_0 \in \mathbb{R}^+$  is such that the poles of  $G_M(s-q_0)$  and the eigenvalues of  $(F+q_0I)$  are stable and  $\delta_2$  $\geq 0$ . p<sub>0</sub> > 0 is defined in S4 and  $\sigma$  in (23) can be expressed as

$$
\sigma = \begin{cases}\n0 & \text{if } \|\theta\| < M_0 \\
\sigma_0 \left(\frac{\|\theta\|}{M_0} - 1\right) & \text{if } M_0 \le \|\theta\| < 2M_0 \\
\sigma_0 & \text{if } \|\theta\| \ge 2M_0\n\end{cases}
$$
\n(28)

where  $M_0 > ||\theta^*||$  and  $\sigma_0 > 2\overline{\mu}^2/R^2 \in \Re^+$  are design parameters. As defined in [10], the modified error is given by  $\varepsilon_1 = e_1 + \boldsymbol{\theta}^T \boldsymbol{\zeta} - G_M \boldsymbol{\theta}^T \boldsymbol{w}$  (29)

## VII. EXPERIMENTAL RESULTS

The MMRAC sensorless speed servo was implemented in a PC-based platform driving an induction motor. The motor is a Y-connected, one pole-pair, 0.9 Hp, 3400 rot/min, 380- V/2.7-A type. Motor parameters are obtained by no-load test, locked-rotor test and board data, and are presented in TABLE 1.

The design begins defining the reference model that it imposes the closed-loop dynamic of the system.

$$
G_{\rm M}(s) = \frac{8.2 \, s + 0.01}{s^2 + 8.2 \, s + 0.01} \tag{30}
$$

Using the parameters presented in TABLE 1, the mechanical plant  $G_0(s)$  is given by

$$
G_0(s) = \frac{1/J}{s + B/J} = \frac{2702.7}{s + 2.702}
$$
 (31)

Note that there is a large difference between the dynamic of the model reference, and the dynamic of the plant, which may cause problems in the MMRAC controller. Moreover, it is necessary that  $n>1$  to enable the use of filters (20) and (21), [10]. To overcome these problems a pre-compensator  $G<sub>C</sub>(s)$  is used.

$$
G_C(s) = \frac{0.009 s + 0.01}{s}
$$
 (32)

The gains  $F$  and  $q$  used in (20) and (21) are equal to 10 and 1, respectively. The DC bus is limited in 170V/5A, as a consequence, the reference speed is 60 rad/s limited. The sampling time used is 555 us and the reference signal is kept at zero until 4s to ensure magnetization of the machine.

Before driving the proposed servo system, it is necessary to obtain experimentally the initial control law parameters  $\theta$ (0) by using a tachometer to feedback the control law MMRAC. In this case, the estimated signal is replaced by the measured rotor speed  $\omega_R$  and the constant  $\sigma_R$  is set equal to 1 during the test. The MMRAC parameters are given in TABLE 3 and  $\boldsymbol{\theta}(0) = \begin{bmatrix} -5 & 5 & -5 & -5 \end{bmatrix}^T$ , which norm is bigger than  $M_0$ . Figure 3 presents the speed servo response using a speed sensor to a reference step. At the final of this test, the MMRAC control law parameters are obtained, Figure 4. Then  $\theta(0) = [-2.63 \ 2.44 \ 1.82 \ -2.8]^\text{T}$  that will be used in the proposed encoderless servo system.

Figures 6-8 show the speed sensorless controller responses obtained using the reference presented in Figure 5. In a first test, the system is initially operating at 0 rad/s, when the speed reference is increased until 60 rad/s. After 10 sec, the speed reference is reduced to -30 rad/s. It can be seen that some spikes are presented in the speed estimated during low speed. These spikes cause some oscillations at d-axis and qaxis currents, as shown in Figure 7. Note that these oscillations do not degrade the control action, Figure 6.

Figures 10-12 show the proposed controller responses using the reference presented in Figure 9. The system is initially operating at 0 rad/s, when the speed reference is increased until 60 rad/s. After 10 sec, the speed reference is reduced to 0 rad/s, and finally it is increased to 30 rad/s. Figure 11 presents the control law parameters obtained and Figure 12 shows the direct and quadrature currents. The actual and estimated speed signals agree quite well for both steady state and transient condition and good accuracy is obtained for this condition, Figure 10.

Figures 13 and 14 present the results obtained in a comparison test between the proposed controller response and the RLS estimator proposed in [12]. In this case, several reference steps are used, including low and zero speed. The system is initially operating at 0 rad/s, when after 4 s, the speed reference is increased from 10 rad/s in each 8 s. Figure 13 presents the measured speed and model reference output. This response is obtained using the MMRAC controller. Note the good accuracy obtained for this condition. Figure 14 presents the estimated signal using the technique proposed in [12]. In speed reference above 10 rad/s the RLS estimator presents good response. However, in condition below 10 rad/s, a wrong estimated signal is presented, as can be verified in Figure 14. It disables the direct feedback of this signal. These results are obtained with no load.

For the load step test, a DC generator (the parameters of which are given in TABLE 2) is connected to the IM rotor. The system is initially operating at 0 rad/s, when the speed reference is increased to 60 rad/s. During the test, a 15  $\Omega$ resistance is connected on the generator terminals in 20 sec. Figure 15 shows the performance in an instantaneous load torque change and Figure 16 presents the quadrature current obtained.















Fig. 3. Servo response using a speed sensor



Fig. 4. Experimental parameters of the MMRAC control law

## VIII. CONCLUSION

This paper described a modified model reference adaptive controller (MMRAC) applied to a speed sensorless servo system using three-phase induction motor. A speed estimator was incorporated in the control system to avoid the use of mechanical sensors. Experimental results demonstrated the effectiveness of the proposed control scheme, including the control at low speed and compensation of torque disturbances.

Moreover, the proposed scheme can be designed for a reduced order plant, without a priori knowledge of the exact model of the plant and the PWM inverter. In contrast with other RMRAC controllers, this scheme does not use measurements of the plant output signal to control it, but uses an observed signal  $\hat{\omega}_R$ .



Fig. 5. Reference signal of the first test



Fig. 6. Estimated speed (solid line)and measured speed (dashed line) in first test



Fig. 7. Control law parameters during the first test



Fig. 8. Quadrature current obtained during the first test



Fig. 9. Reference signal in the second test



Fig. 10. Estimated speed (solid line)and measured speed (dashed line) in second test

## ACKNOWLEDGEMENT

The authors would like to express their gratitude to the Coordination of Personnel Improvement at Superior Level (CAPES) and the National Council of Scientific and Technological Developments (CNPq) for their financial support.



Fig. 11. Control law parameters during the second test



Fig. 12. Quadrature current obtained during the second test



Fig. 13. Measure speed (solid line) and model reference output (dotted line) in a comparison test

# APPENDIX

**Lemma 1:** Let  $C(t)$  given by (9) where  $V_{ds}$ ,  $V_{gs}$ ,  $I_{ds}$ ,  $I_{qs}$  and them derivates are piecewise continuous function of time Moreover, consider the linear error equation  $e_L = (\hat{\omega}_R - \omega_R)C(t)$  (vide [2] eq. 2.4.3) with a RLS



Fig. 14. Estimated speed (solid line) and model reference output (dotted line) in a comparison test



Fig. 15. Estimated speed (dashed line ), measured speed (solid line) and model reference speed (dotted line) in torque disturbance test



Fig. 16. Quadrature current obtained during the torque disturbance test

algorithm presented in (8)-(14) and  $\sigma_R = 1$ . Defining a vector  $C: \Re_+ \to \Re^{2n}$ , so

a) 
$$
\frac{e_L}{\sqrt{1 + C^T P_R C}} \in L_2 \cap L_\infty
$$
  
b) 
$$
\overline{\omega}_R \in L_\infty, \overline{\omega}_R \in L_2 \cap L_\infty
$$

c) 
$$
\beta = \frac{\overline{\omega}_R \mathbf{C}}{1 + ||\mathbf{C}_T||_{\infty}}, \ \beta \in L_2 \cap L_{\infty}
$$

where  $\overline{\omega}_R = \widehat{\omega}_R - \mathring{\omega}_R$ .  $\beta$  can be considered a normalized error and  $e_L$  is normalized by  $\left\|C_T\right\|_{\infty}$ .  $\beta$  is included in  $L_2$ . This assure that this gain converge to a small value when t→∞. By this way, the output error  $e_L \n\in L_2 \cap L_\infty$ ,  $e_L \to 0$  when  $t \rightarrow \infty$ . Moreover, the derivate of the parametric error  $\vec{\omega}_R \in L_2 \cap L_\infty$  and  $\vec{\omega}_R \to 0$  when  $t \to \infty$ .

**Proof of Lemma 1:** The proof of Lemma 1, that assure the convergence of  $\overline{\omega}_R$ , can be found in Bodson [2] theorem 2.4.4, and here will be omitted.

 $\Box$ 

When  $\omega_{RM}$  is smaller than  $M_{R0}$ ,  $\sigma_R = 0$ , the signal used in the control law feedback is  $\omega_{RM}$ . In this case, the real control law parameters  $\theta$  need to be known. To obtain them it is necessary to use a tachometer, as presented in section VII.

## **REFERENCES**

- [1] K. Minami, M. V. Reyes, G. C. Verghese, "Multi-Stage Speed and Parameter Estimation for Induction Machines", *IEEE Annual Power Electronics Specialists Conference PESC*, pp. 596-604, 1991
- [2] M. Bodson, S. Sastry, *Adaptive Control: Stability, Convergence, and Robustness*, Prentice Hall, New Jersey, 1989.
- [3] J. L. Mora, A. Torralba, L. G. Franquelo, "An adaptive speed estimator for induction motors based on a Kalman filter with low sample time", *IEEE* 32nd *Annual Power Electronics Specialists Conference PESC*, vol.2, 794-798, June 2001.
- [4] L.Salvatore, S. Stasi, and F. Cupetino, "Improved rotor speed estimation using two Kalman filter-based algorithms", *in Conf. Rec. IEEE-IAS Annual Meeting*, pp. 125-132, 2001.
- [5] C. Schauder, "Adaptive speed identification for vector control of induction motors without rotational transducers", *IEEE Transactions on Industry Applications*, vol. 28, pp. 1054-1061, September/October 1992
- [6] L. Zhen, and L. Xu, "Sensorless field orientation control of induction machines based on mutual MRAS scheme", *IEEE Transactions on Industrial Electronics*, vol. 45, pp. 824-831, October 1998.
- [7] C. Lascu, I. Boldea, and F. Blaabjerg, "A modified direct torque control for induction motor sensorless drive", *IEEE Transactions on Industrial Electronics*, vol. 36, pp. 122-130, February 2000.
- [8] C. B. Jacobina, A. M. N. Lima, and F. Salvatori, "Flux and torque control of an induction machine using linear discrete state space approach", *IEEE International Conference on Industrial Electronics, Control and Instrumentation IECON*, vol. 2, pp. 511-516, November 1997.
- [9] P. A. Ioannou, K. S. Tsakalis, "A robust direct adaptive controller", *IEEE Transactions on Automatic Control*, vol.31, pp.1033-1143, November 1986.
- [10] R. L.-Leal, J. Collado, S. Mondié, "Model reference robust adaptive control without a priori knowledge of the high frequency gain", *IEEE Transactions on Automatic Control*, vol.35, pp. 71-76, January 1990.
- [11] W. Leonard, *Control of Electrical Drives*, Sprinter, Berlin, 1996.
- [12] M. V. Reyes, K. Minami, G. C. Verghese, "Recursive Speed and Parameter Estimation for Induction Machines", in *Conf. Rec. IAS*, pp. 607- 611, 1989.
- [13] A. Consoli, G. Scarcella, A. Testa, "A new zerofrequency flux-position detection approach for direct-field-oriented-control drives", *IEEE Transactions on Industry Applications*, vol.36, No.3, pp. 797-804, 2000.
- [14] P. L. Jansen, R. D. Lorenz, "Transducerless position and velocity estimation in induction and salient AC machines", *IEEE Transactions on Industrial Electronics*, vol.31, pp. 240-247, 1995.
- [15] Y. D. Landau, *Adaptive Control: The Model Reference Approach*, Marcel Dekker, 1979.

## BIOGRAPHIES

**Helder T. Câmara**, was born in Natal, RN, Brazil, in 1977. He received the B.S. and M.S. degrees in electrical engineering from the Federal University of Santa Maria, Santa Maria, Brazil, in 2000 and 2002, respectively, where he is currently pursuing the Ph.D. degree in electrical engineering. His research interests include digital control techniques of motor drives, robust adaptive control, and control systems applications.

Mr. Câmara is currently a member of the IEEE Industry Applications Society.

**Hilton A. Gründling**, was born in Santa Maria, RS, Brazil, in 1954. He received the B.S. degree from the Pontifical Catholic University of Rio Grande do Sul, Porto Alegre, Brazil, in 1977, the M.S. degree from the Federal University of Santa Catarina, Santa Catarina, Brazil, in 1980, and the Ph.D. degree from the Technological Institute of Aeronautics, São Paulo, Brazil, in 1995.

Since 1980, he has been with the Federal University of Santa Maria, Rio Grande do Sul, Brazil, where he is currently a Professor. His research interests include robust model reference adaptive control, discrete control, and control systems applications